

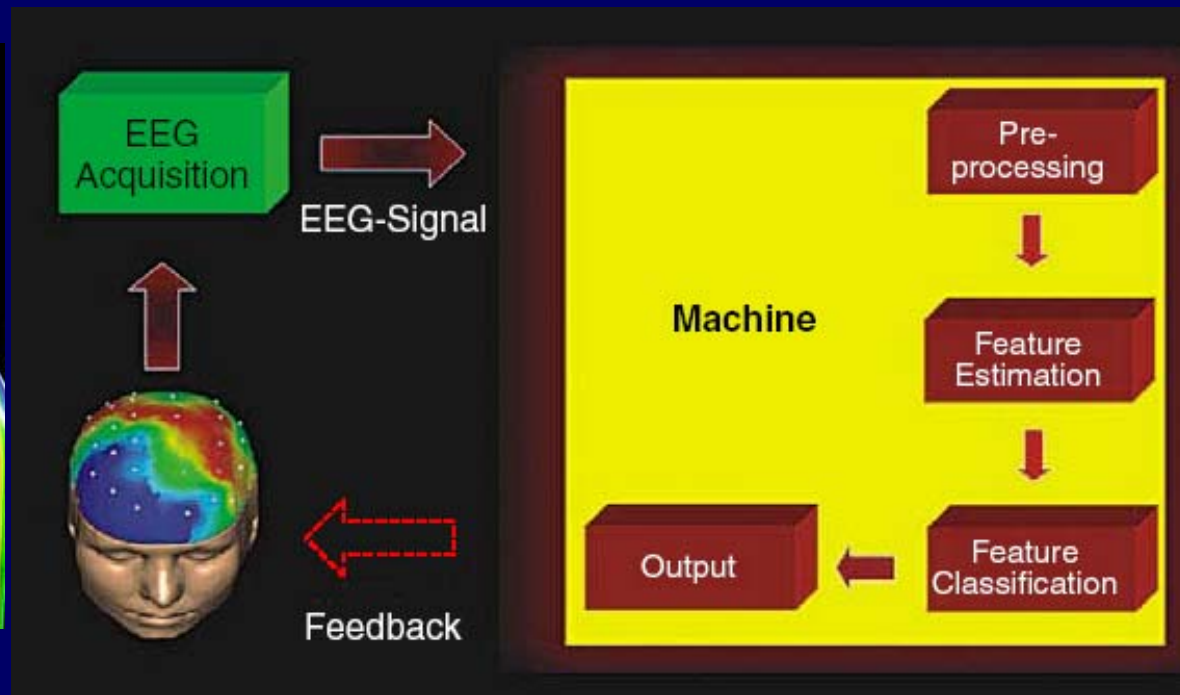
# DSP概論： Biomedical Signal Processing

台大電機系 李百祺

# Brain-Machine Interface

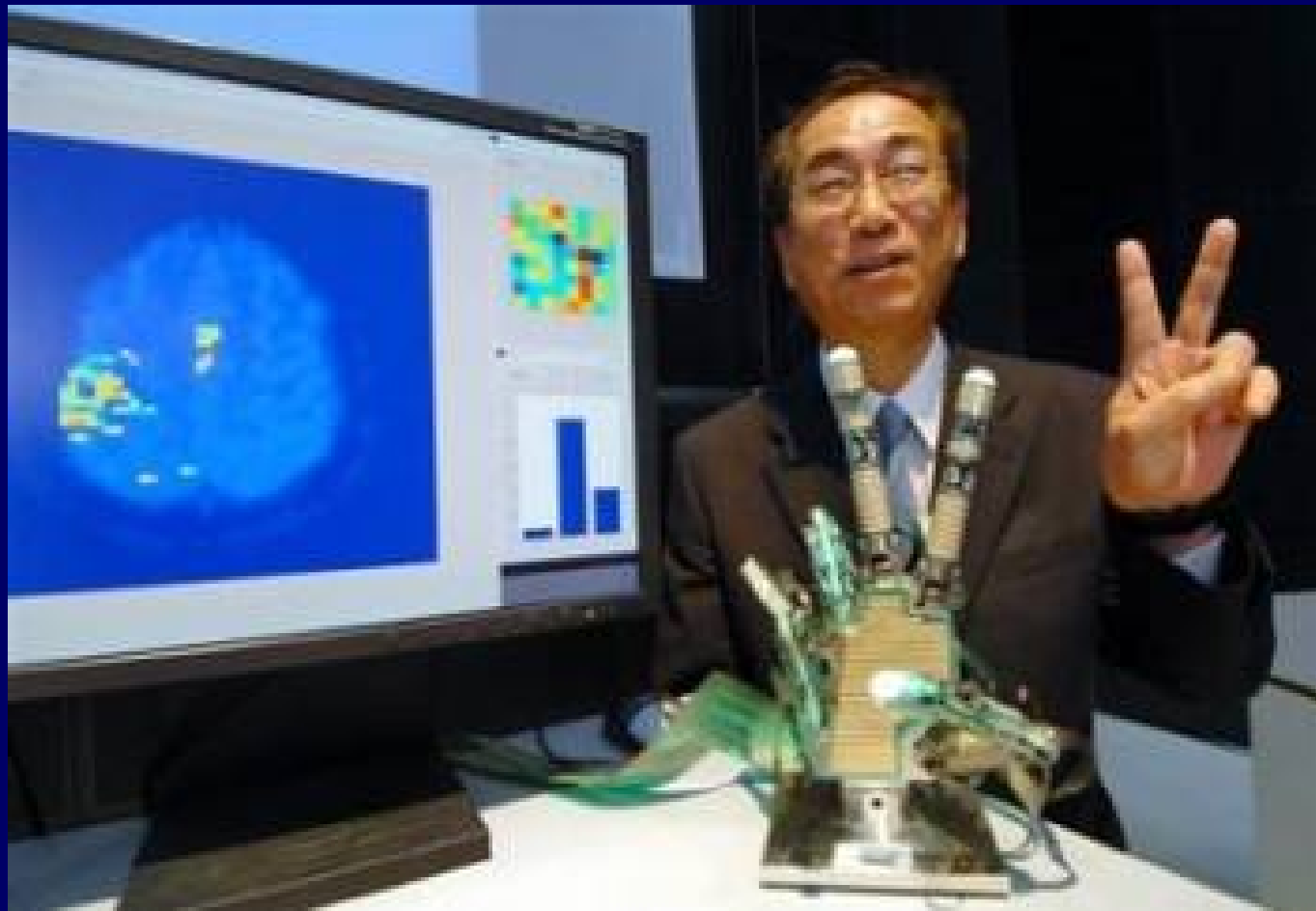


# Brain-Machine Interface

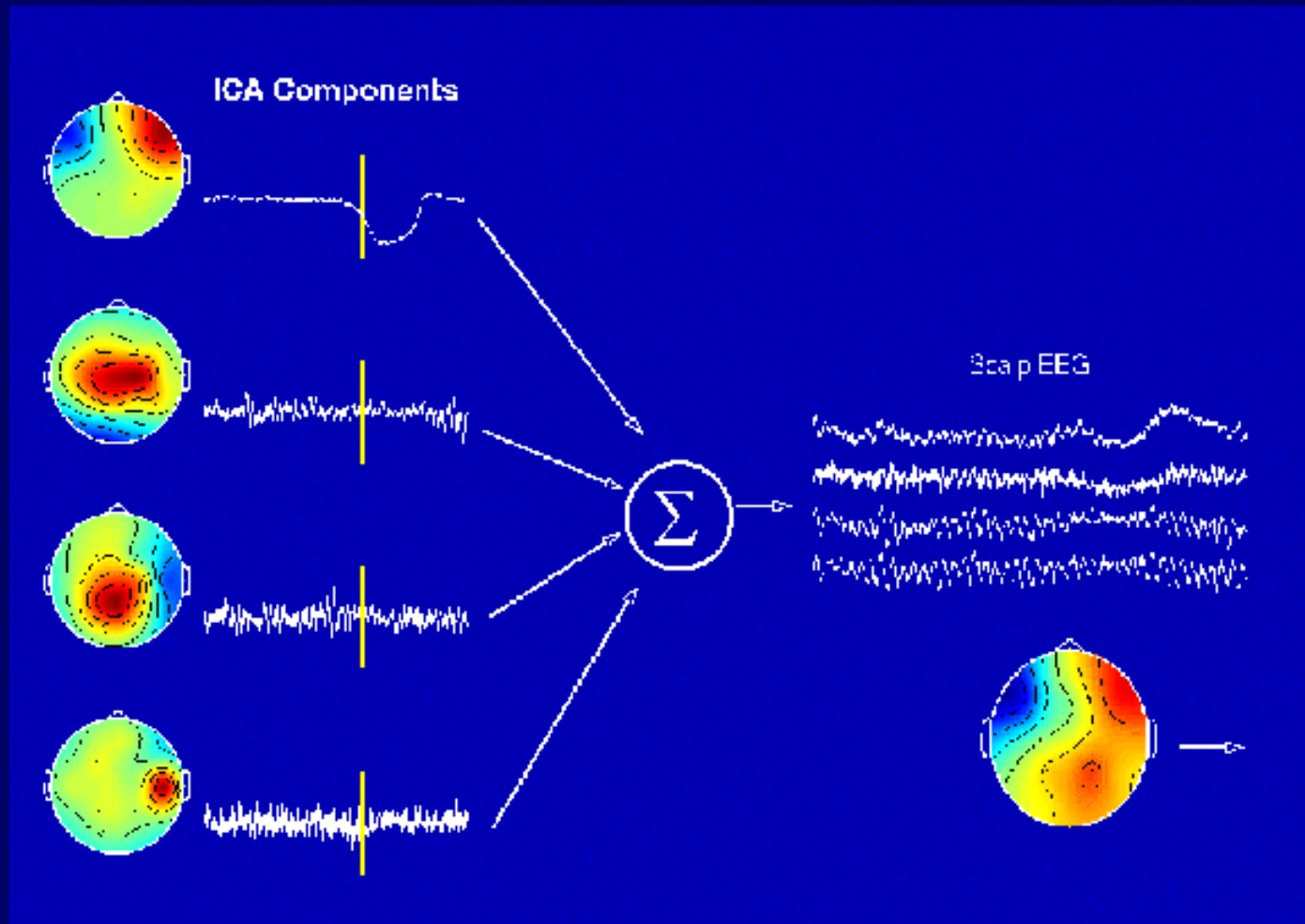


# Brain-Machine Interface

(By ATR-Honda)



# The Need for Biomedical Signal Processing

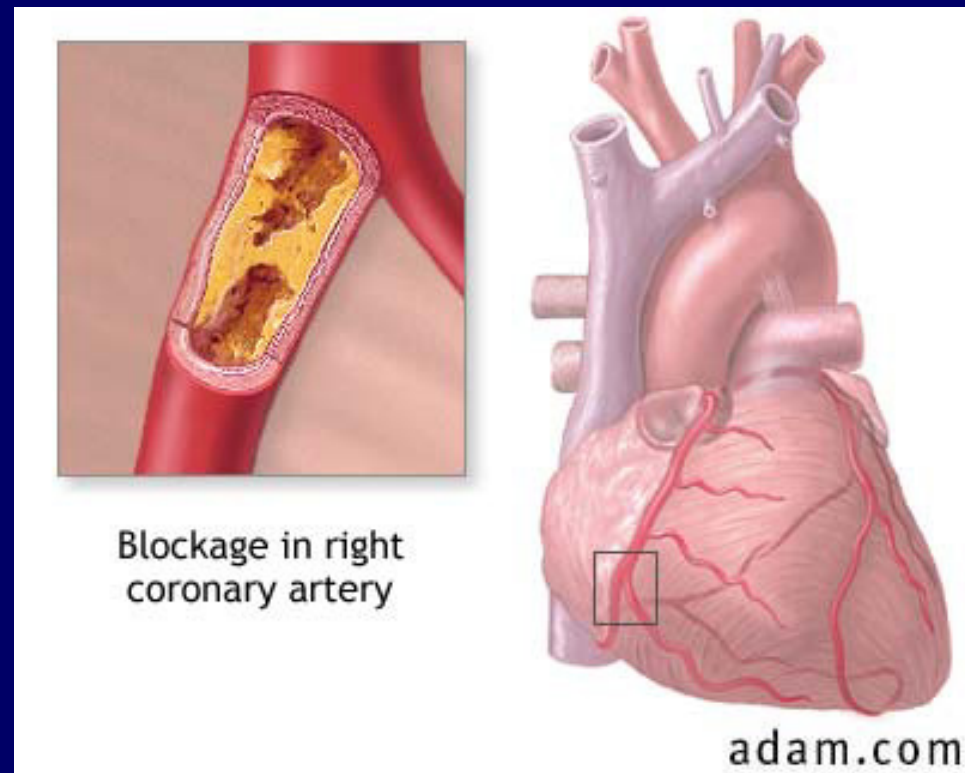


# What is it?

- Biomedical Signal Processing: Application of *signal processing methods*, such as filtering, Fourier transform, spectral estimation and wavelet transform, to *biomedical problems*, such as the analysis of cardiac signals, the breathing cycle,...etc.
- A broader aspect: Biomedical imaging, genomic signal processing,...etc.

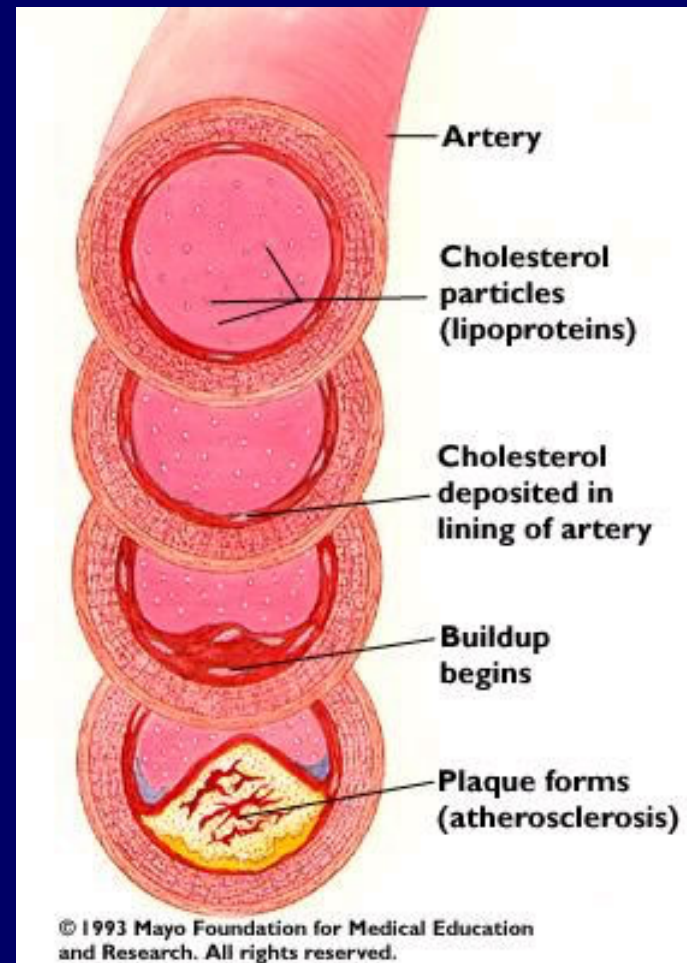
# Medical Diagnosis: Heart Attack as another Example

- Heart attack: Coronary artery disease, blockage of blood supply to the myocardium.



# Medical Diagnosis: Heart Attack as an Example

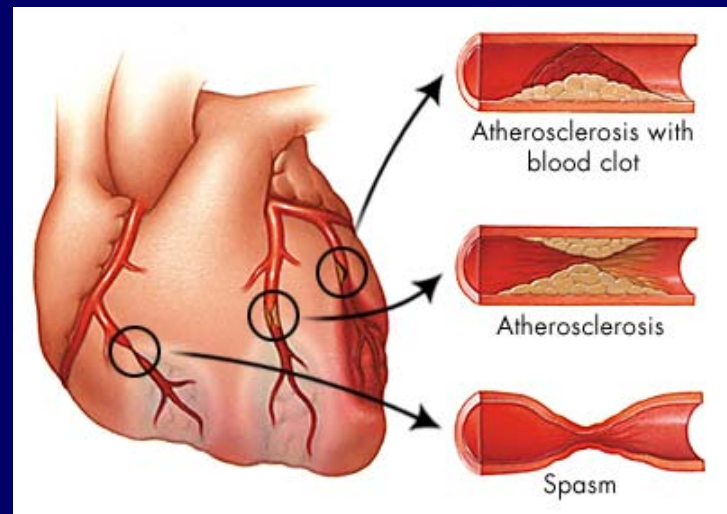
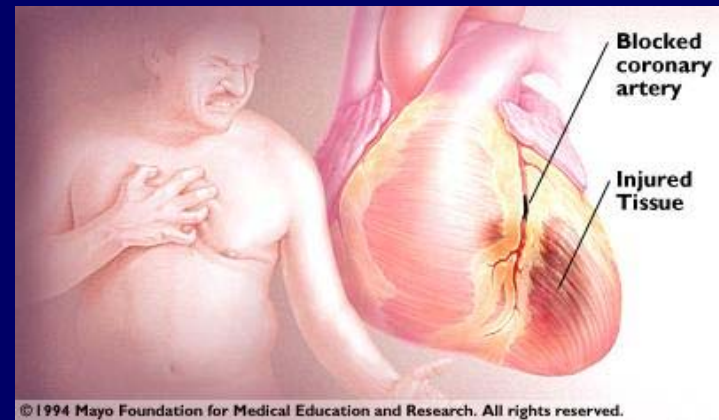
- Plaque: A gradual build-up of fat (cholesterol) within the artery wall.





# Medical Diagnosis: Heart Attack as an Example

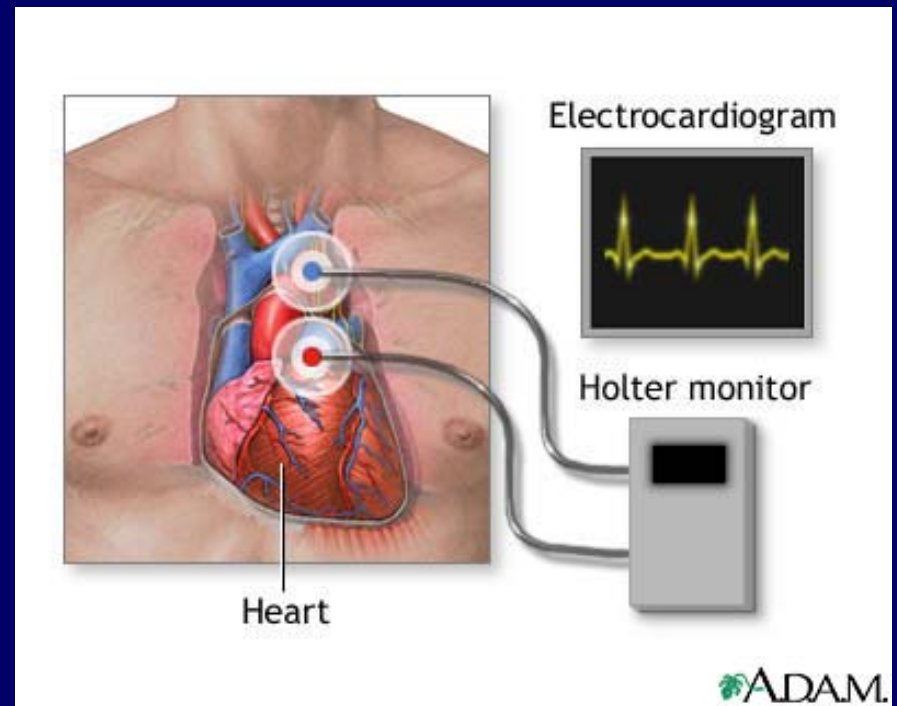
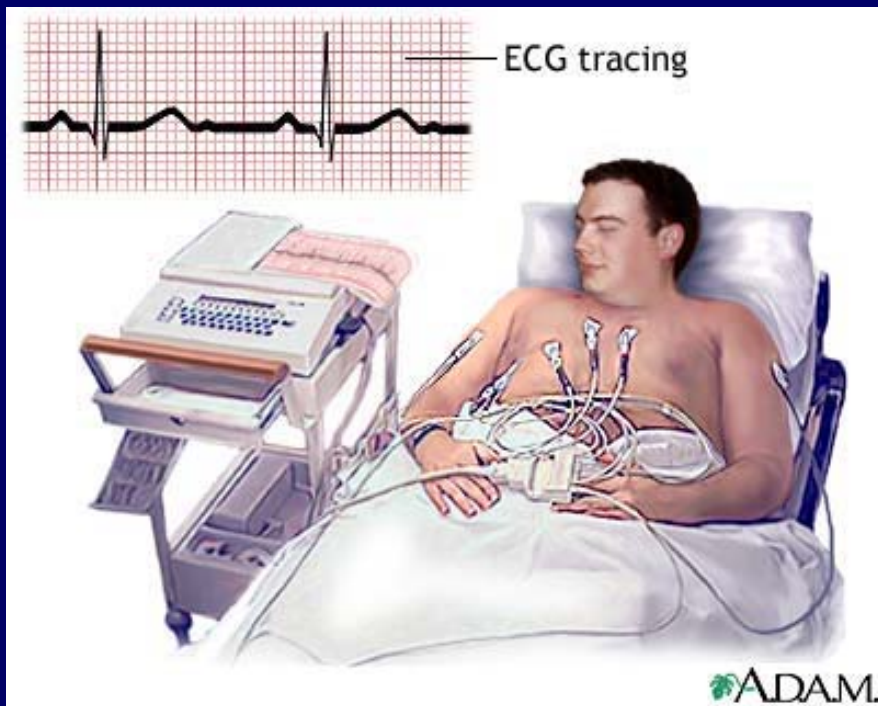
- Symptoms:
  - Chest pressure with stress, heart burn, nausea, vomiting, shortness of breath, heavy sweating.
  - Chest pain, heart attack, arrhythmias.



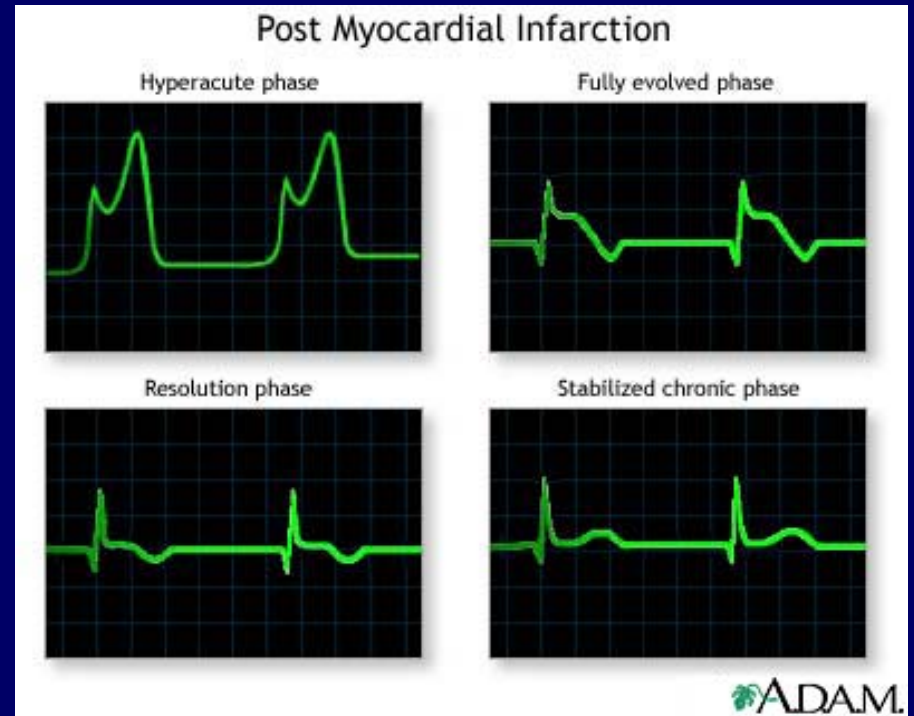
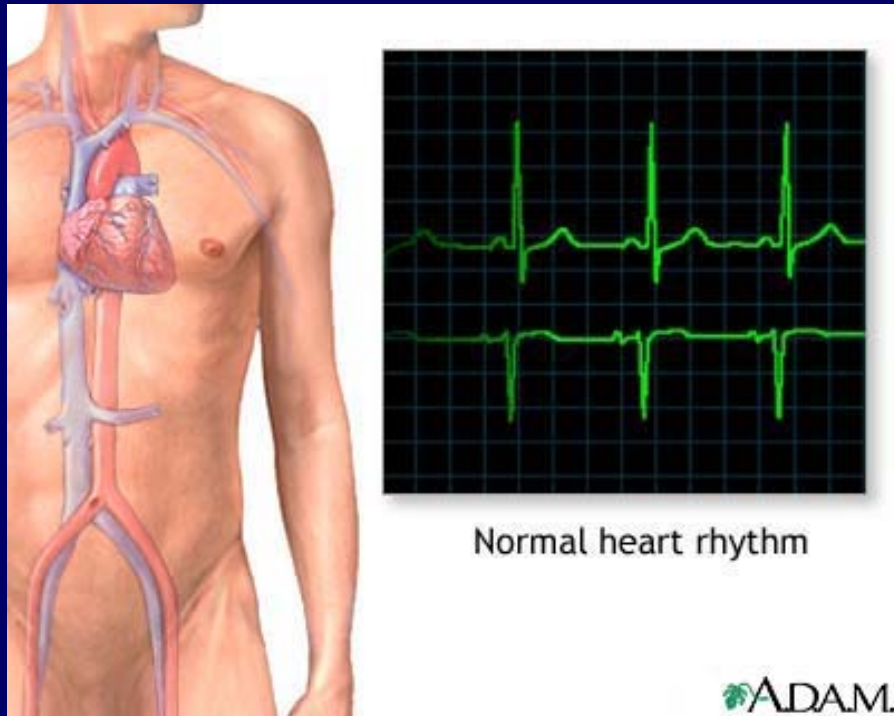
# Medical Diagnosis: Heart Attack as an Example

- Diagnosis:
  - Prehospital electrocardiography (ECG).
  - Continuous/serial ECG.
  - Exercise stress ECG.
  - Biochemical tests and biomarkers.
  - Sestamibi myocardial perfusion imaging.
  - Echocardiography.
  - Computer-based decision aids.

# Medical Diagnosis: ECG



# Medical Diagnosis: ECG



# Medical Diagnosis: ECG

Atrioventricular block ECG tracing



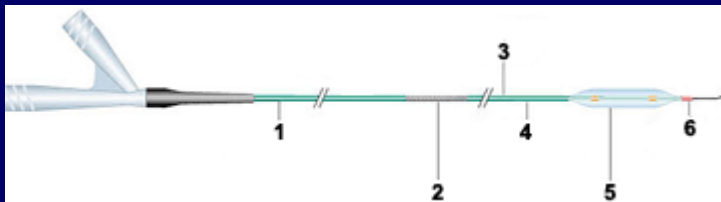
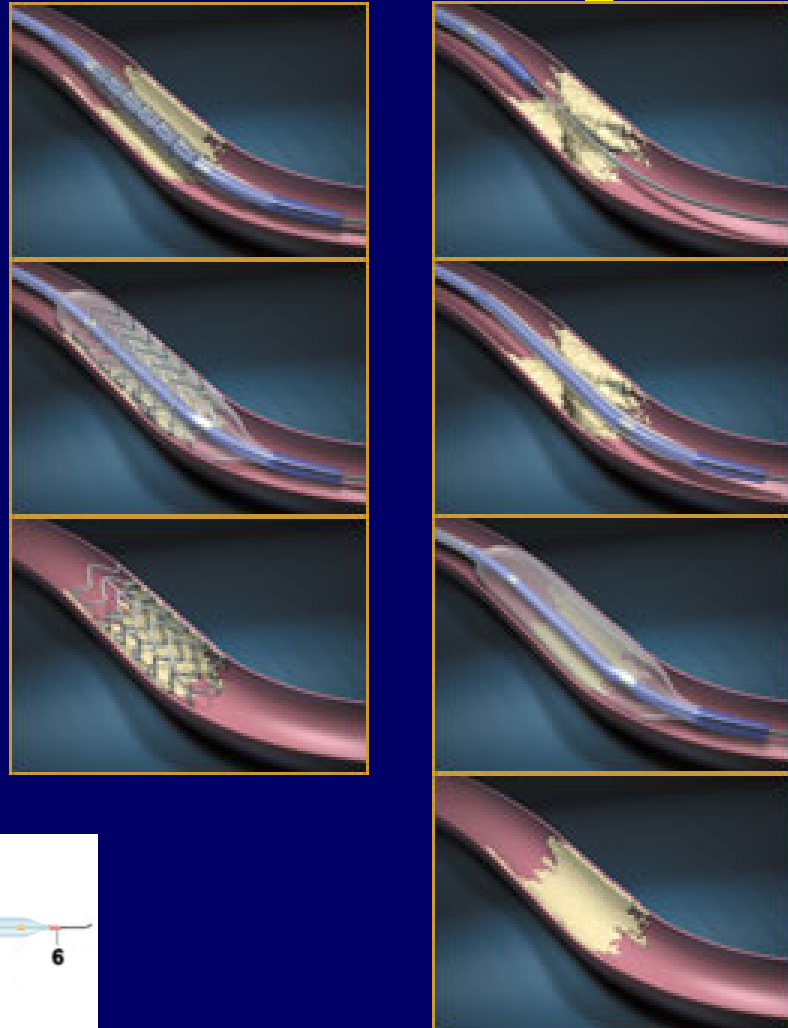
Ventricular tachycardia



# Medical Diagnosis:

## Heart Attack as an Example

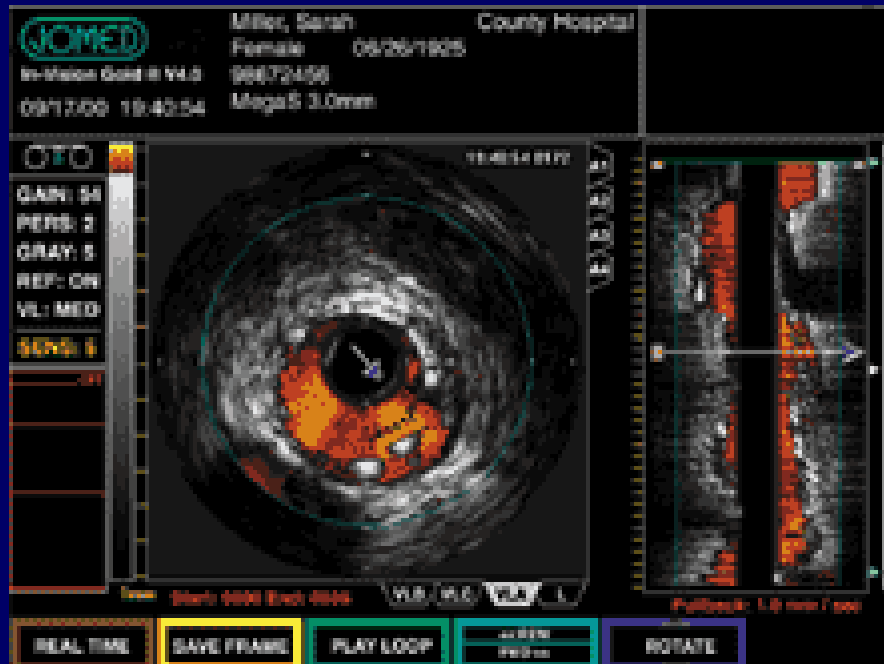
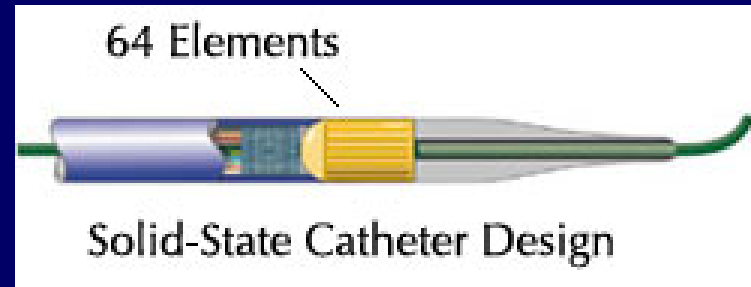
- Treatment:
  - Angioplasty.
  - Stent implantation.
  - Atherectomy.
  - Coronary bypass surgery.
  - Intravascular radiotherapy.
  - Excimer laser.





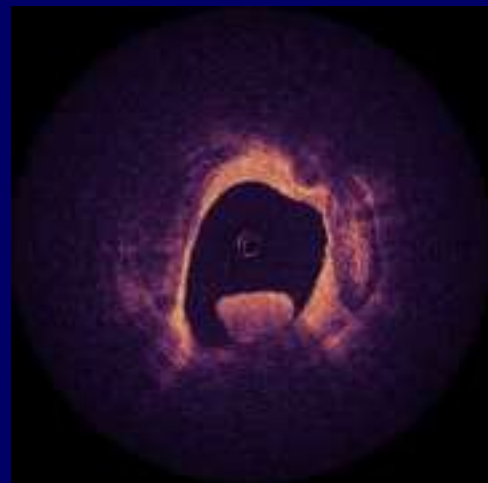
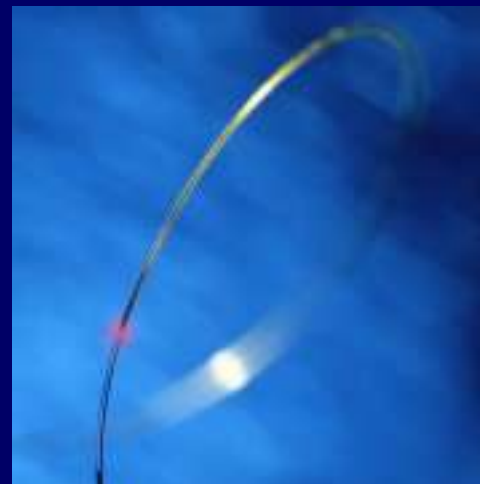
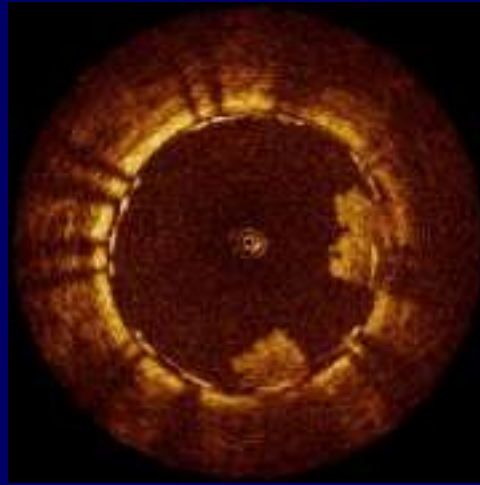
# Medical Diagnosis: Heart Attack as an Example

- Imaging:
  - Ultrasound.



# Medical Diagnosis: Heart Attack as an Example

- Imaging:
  - Optics.





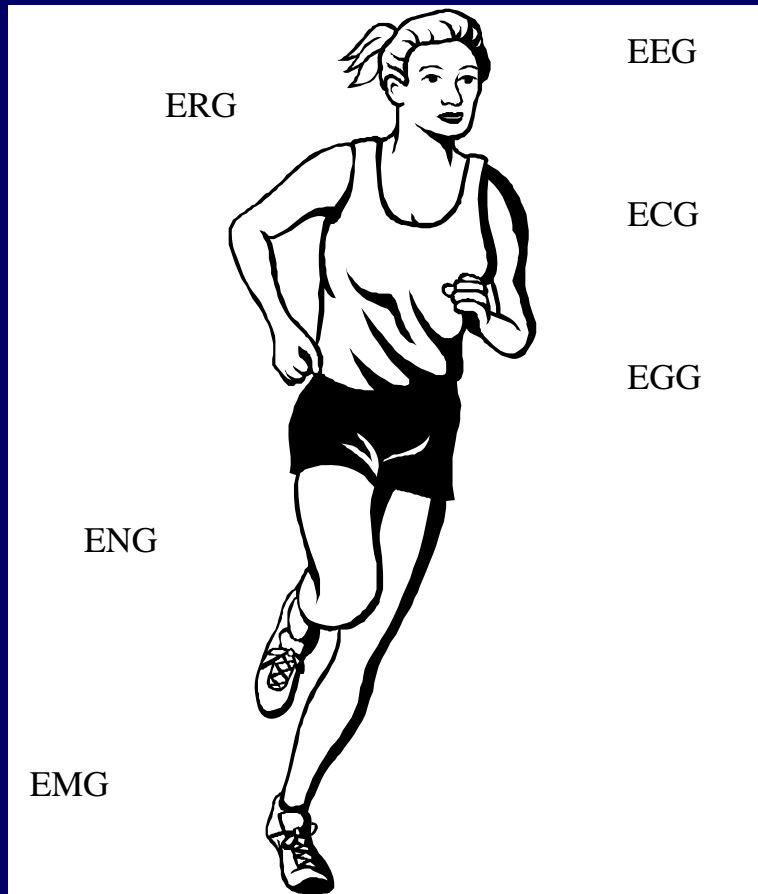
# Biomedical Signals: Broader Definition

- Signals as a result of physiological activities in the body:
  - Electrical and Non-electrical
- Invasive/Non-invasive interrogation of an external field with the body
- Diagnosis and therapy
- ➔ *Will focus mostly on bioelectric signal.*

# Outline

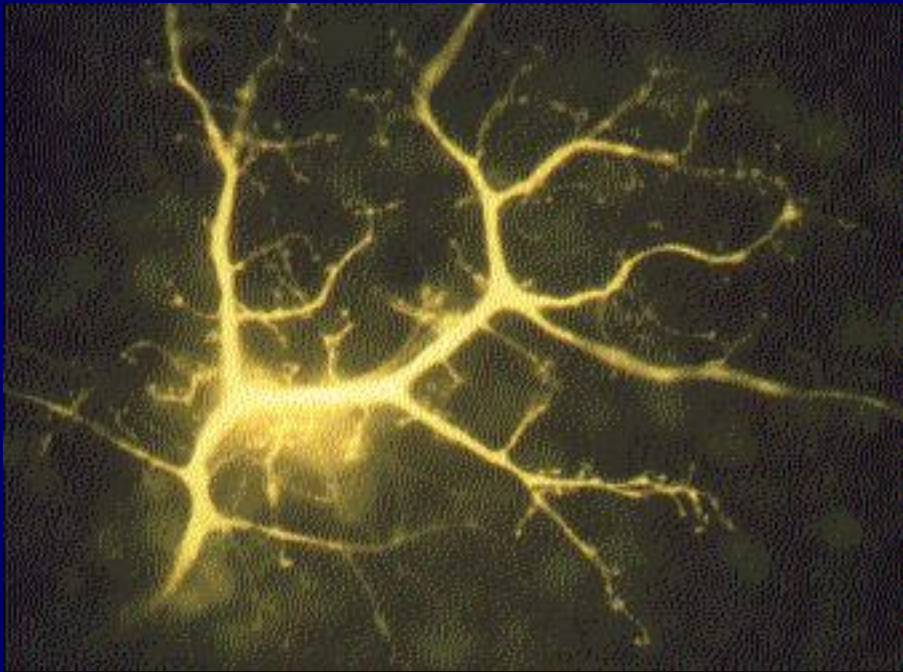
- Bioelectrical signals:
  - Excitable cells
  - Resting/action potential
- ECG, EEG,...etc
- Applications of signal processing techniques
  - Sampling, filtering, data compression,...etc
- Non-stationary nature of biomedical signals

# Bioelectrical Signals

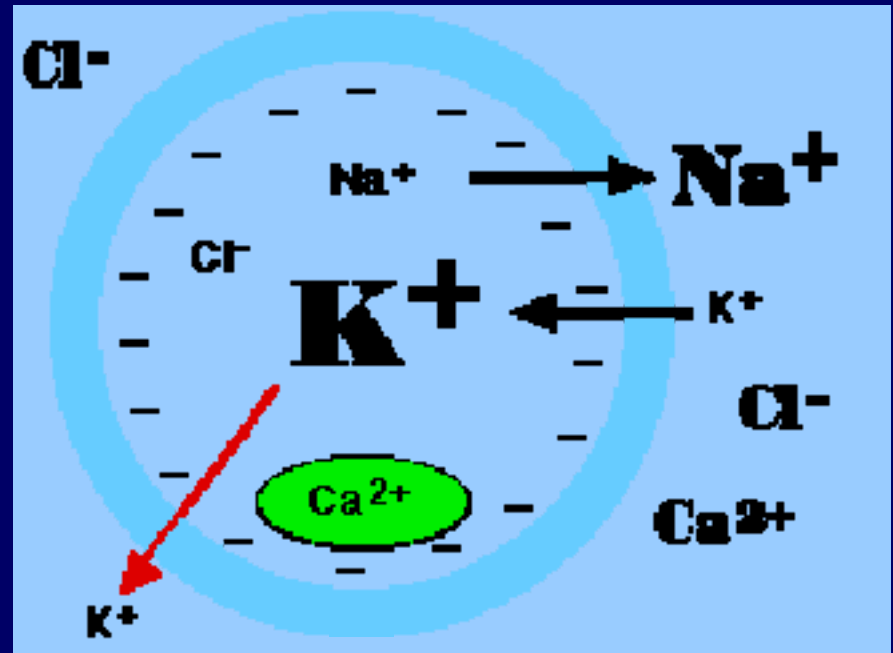


- The bioelectric signals represent many physiological activities.

# Excitable Cells

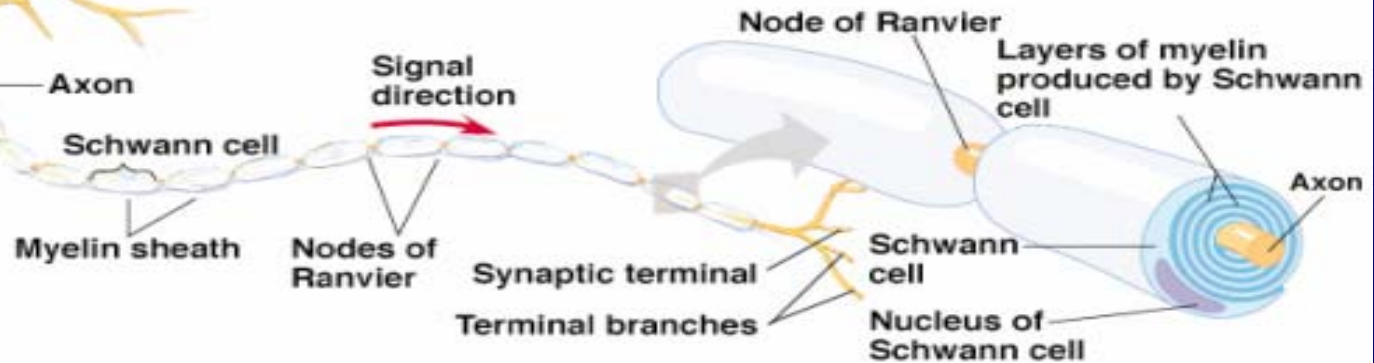
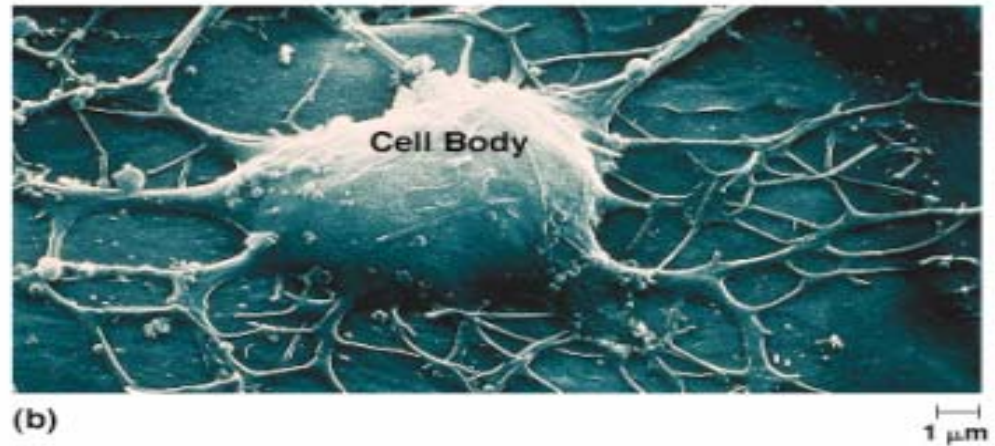
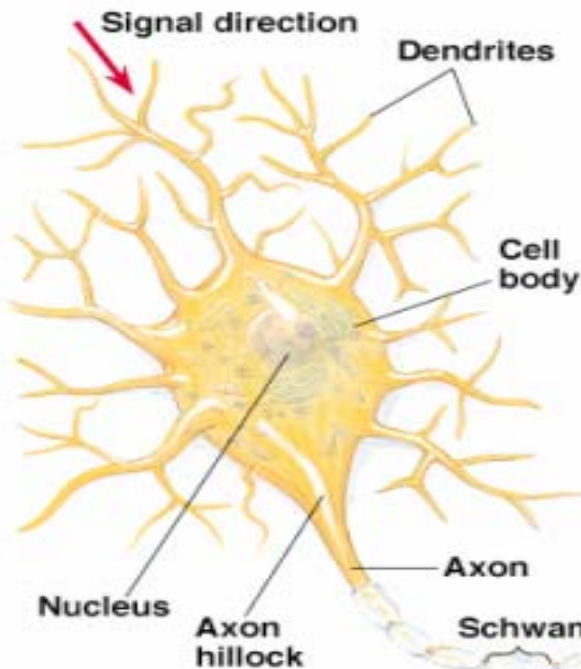


Neuron (Rabbit Retina)

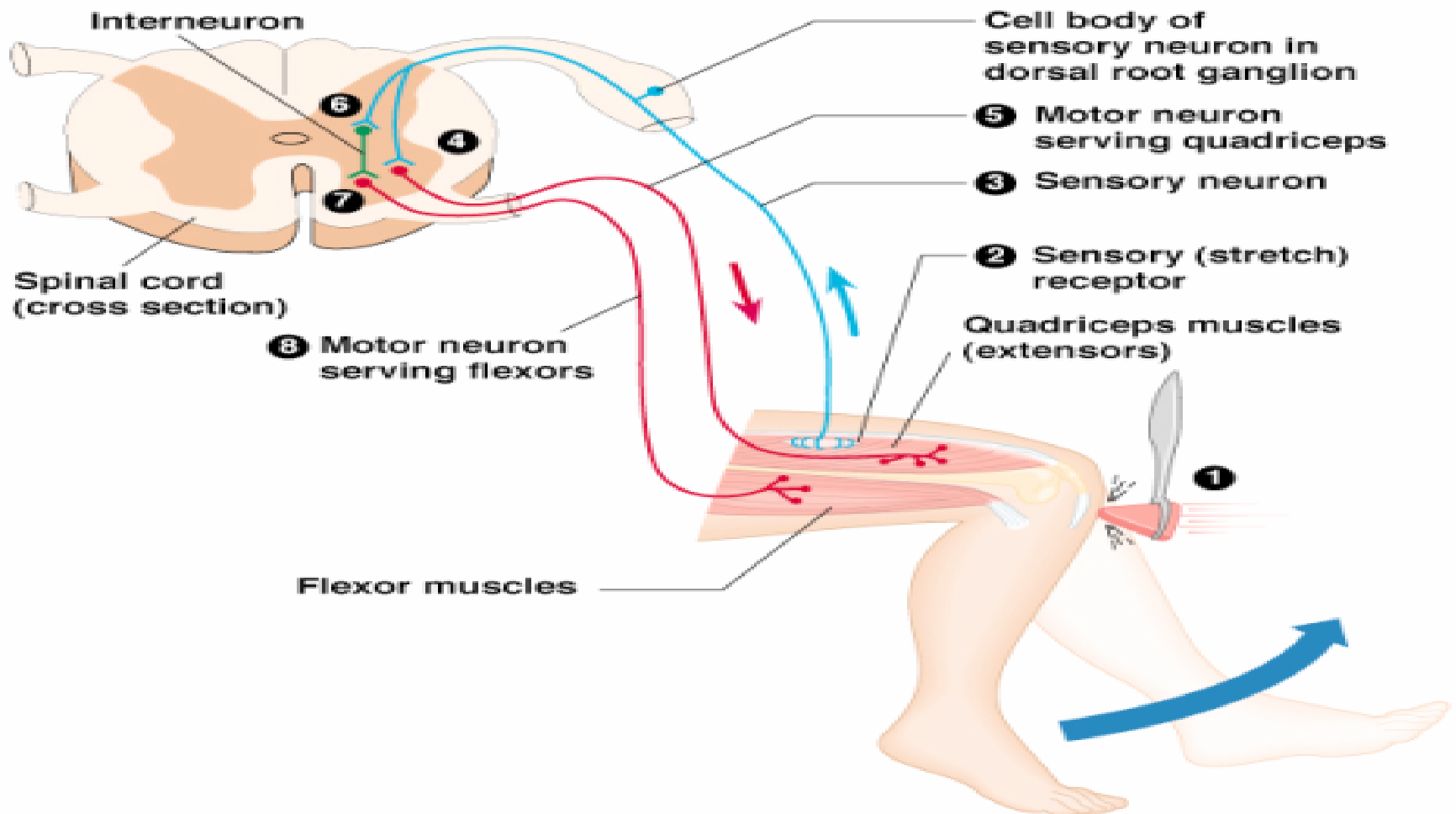


Ionic Relations in the Cell

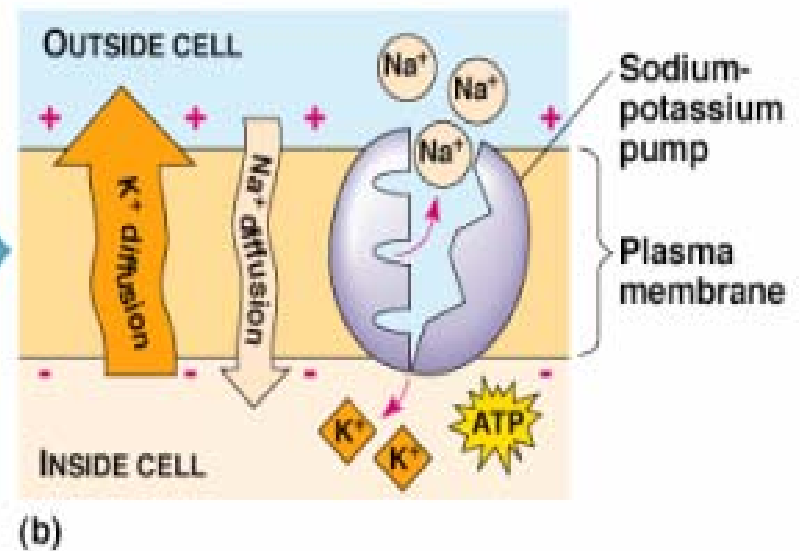
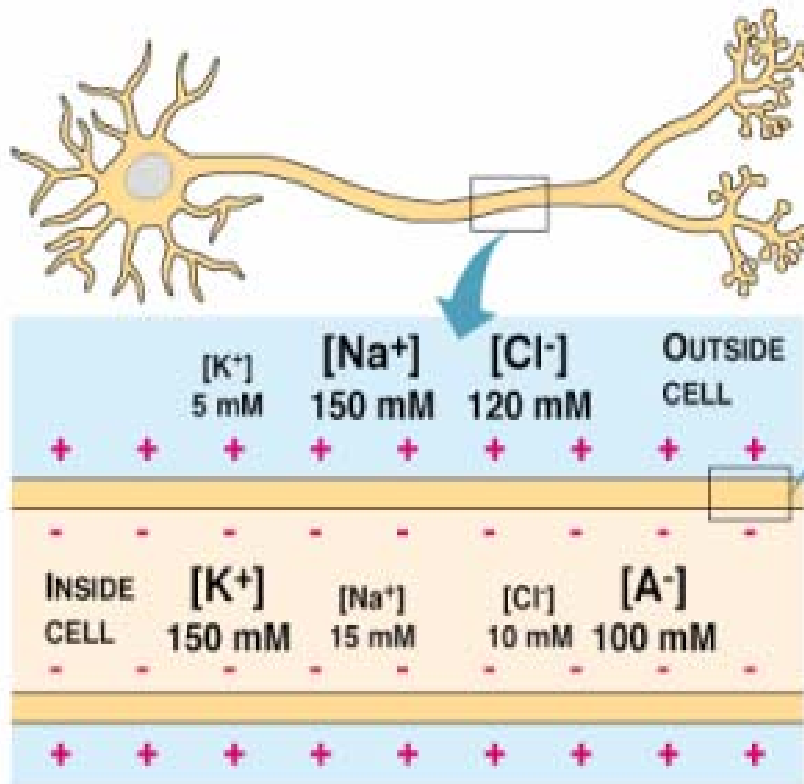
# Structural unit



# Functional unit

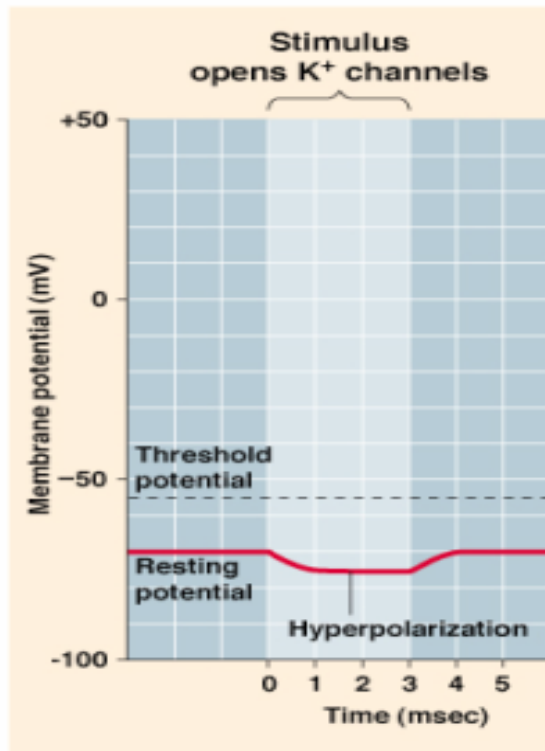


# Neural signaling (I)

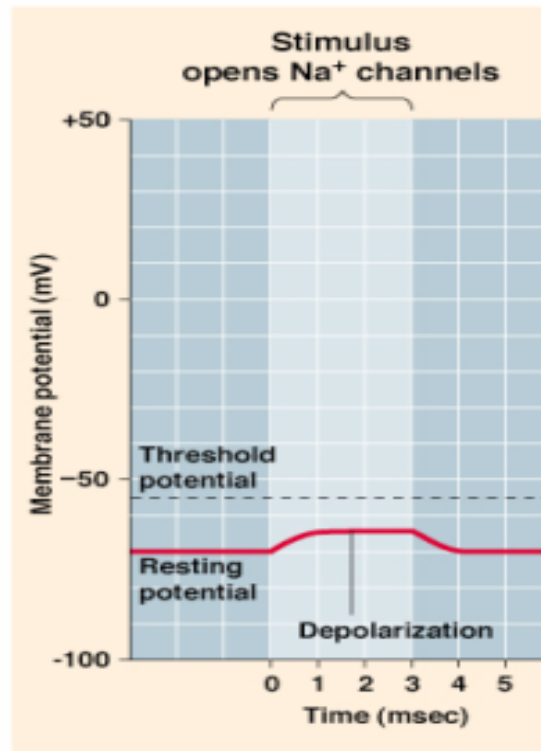


(a)

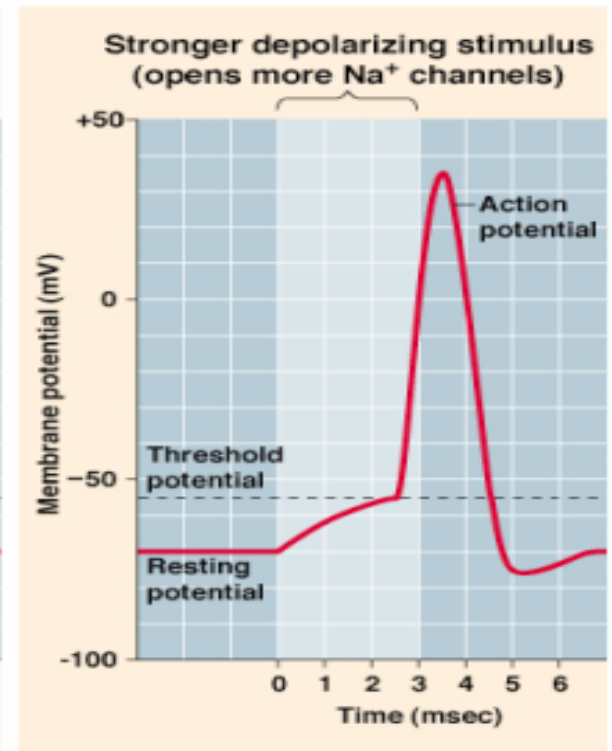
# Neural signaling (II)



(a) Graded potential:  
hyperpolarization



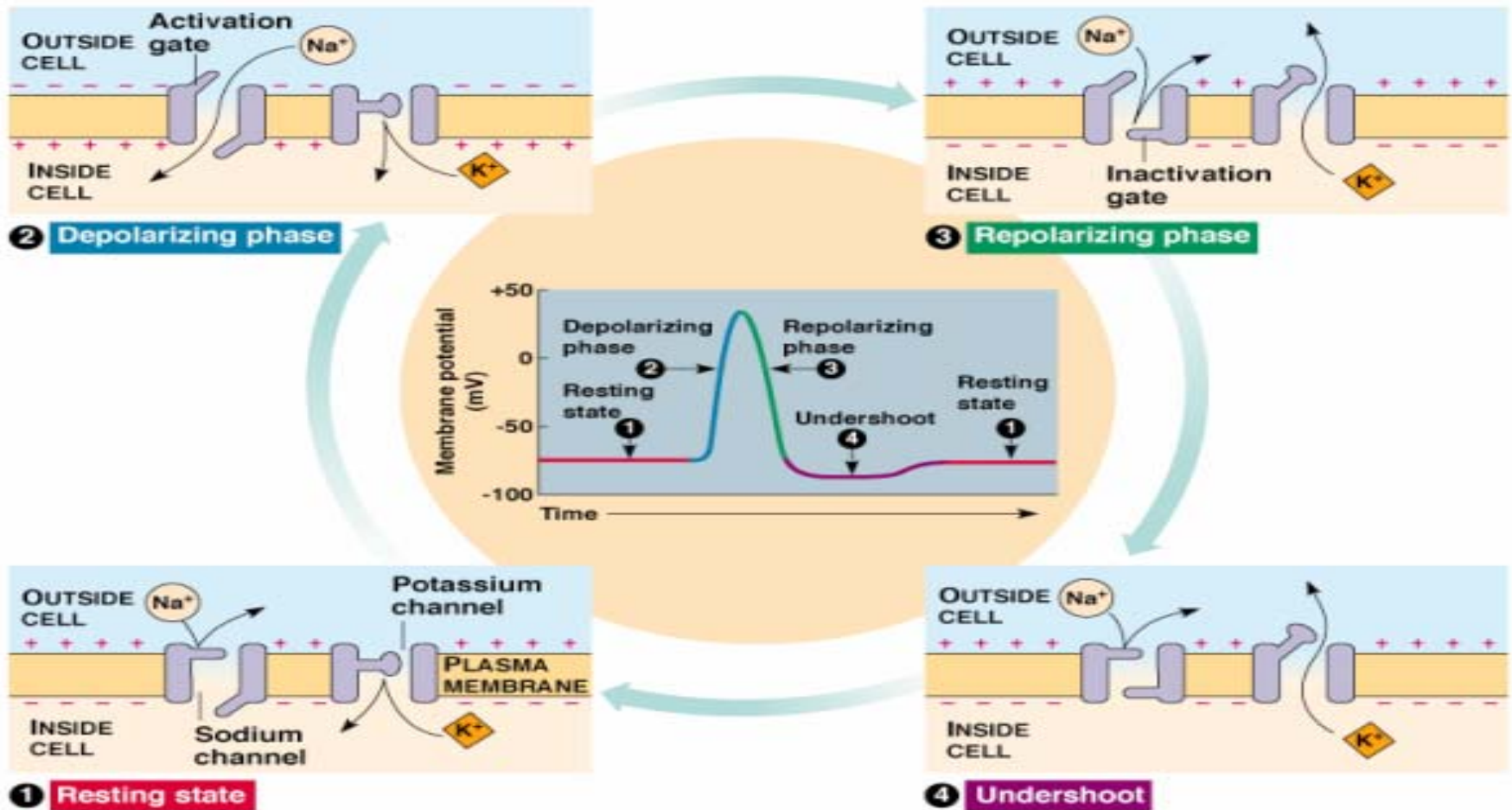
(b) Graded potential:  
depolarization



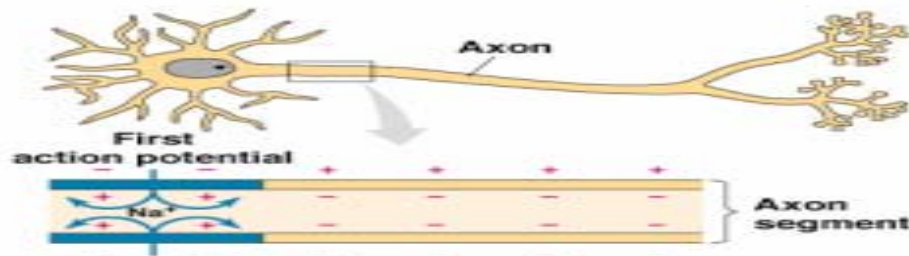
(c) Action potential



# Neural signaling (III)



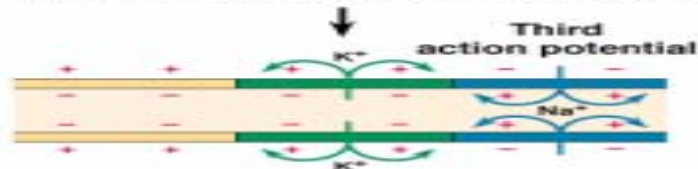
# Neural signaling (IV)



- 1 An action potential is generated as sodium ions flow inward across the membrane at one location.

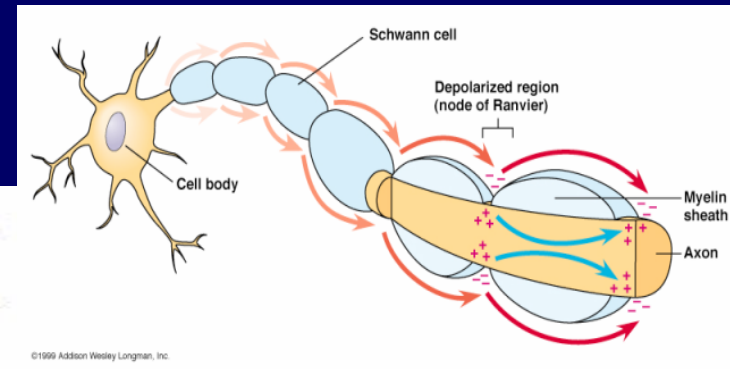


- 2 The depolarization of the first action potential has spread to the neighboring region of the membrane, depolarizing it and initiating a second action potential. At the site of the first action potential, the membrane is repolarizing as K<sup>+</sup> flows outward.



- 3 A third action potential follows in sequence, with repolarization in its wake. In this way, local currents of ions across the plasma membrane give rise to a nerve impulse that passes along the axon.

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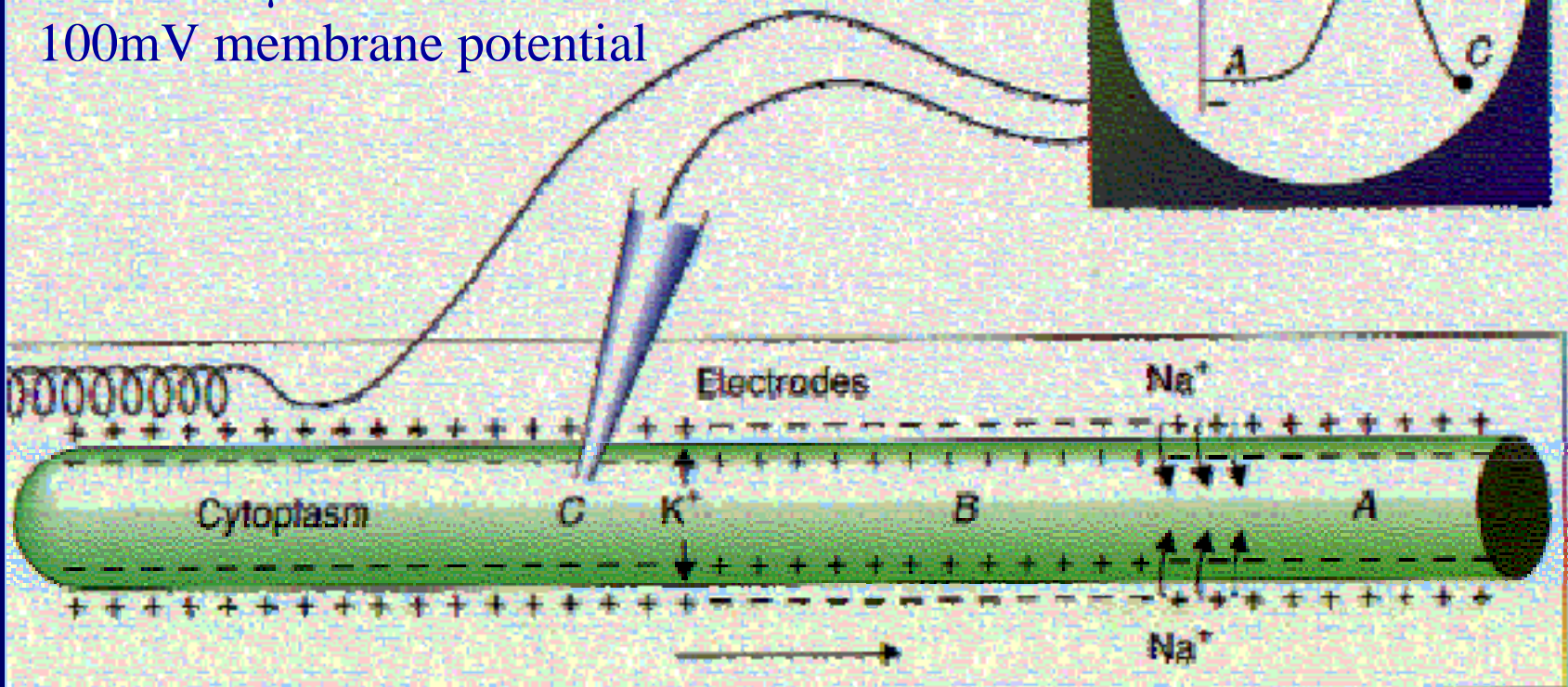
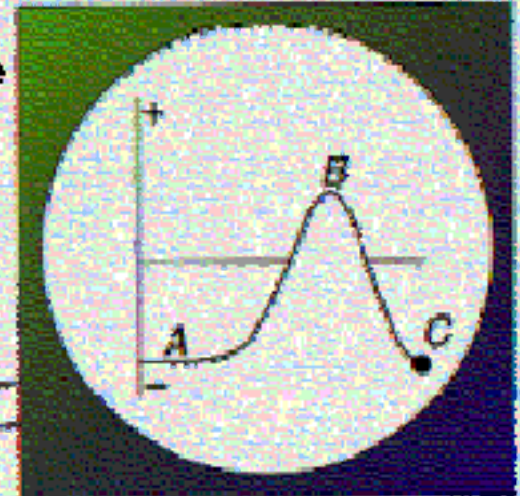
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# Measurements of Action Potential

$$C = \varepsilon \frac{A}{d}$$

6250 ions/ $\mu\text{m}^2$  for  
100mV membrane potential

Oscilloscope



# Goldman Equation

$$E = \frac{RT}{F} \ln \left\{ \frac{P_K [K]_o + P_{Na} [Na]_o + P_{Cl} [Cl]_i}{P_K [K]_i + P_{Na} [Na]_i + P_{Cl} [Cl]_o} \right\}$$

- $E$ : Equilibrium resting potential
- $R$ : Universal Gas Constant (8.31 J/(mol\*K))
- $T$ : Absolute temperature in K
- $F$ : Faraday constant (96500 C/equivalent)
- $P_M$ : Permeability coefficient of ionic species M.

# Example: Ion Concentration

Species	Intracellular (millimoles/L)	Extracellular (millimoles/L)
$\text{Na}^+$	12	145
$\text{K}^+$	155	4
$\text{Cl}^-$	4	120

*(For frog skeletal muscle)*



# Example: Equilibrium Resting Potential for frog skeletal muscle

- $P_{Na} : 2 \times 10^{-8} \text{ cm/s}$
- $P_K : 2 \times 10^{-6} \text{ cm/s}$
- $P_{Cl} : 4 \times 10^{-6} \text{ cm/s}$
- $E = -85.3 \text{ mV}$

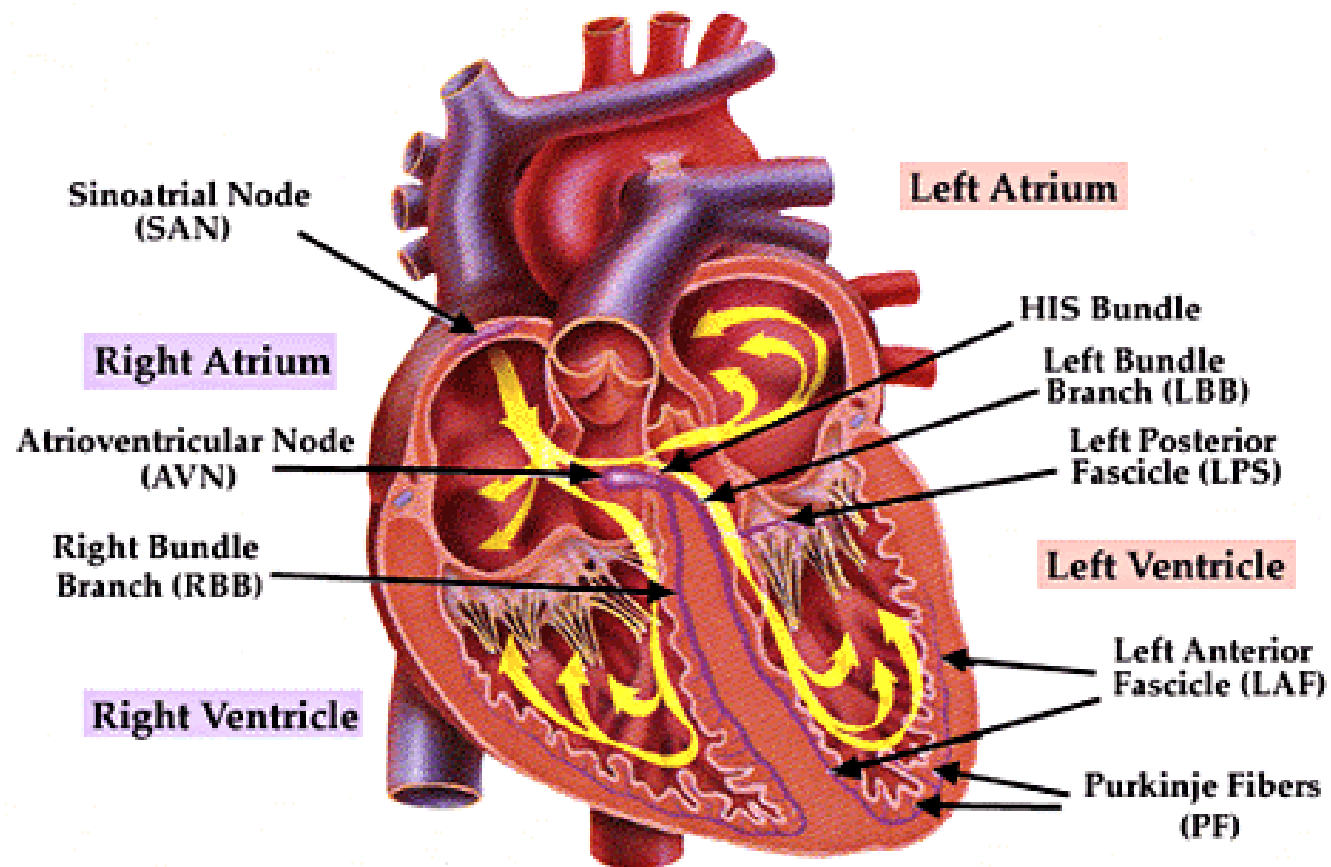
# Electrocardiogram (ECG)

# ECG

- One of the main methods for assessing heart functions.
- Many cardiac parameters, such as heart rate, myocardial infarction, and enlargement can be determined.
- Five special groups of cell:
  - SA, AV, common bundle, RBB and LBB.

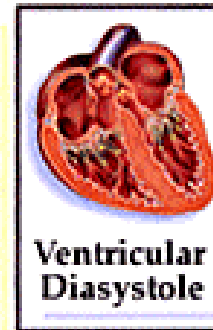
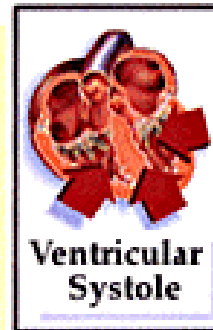
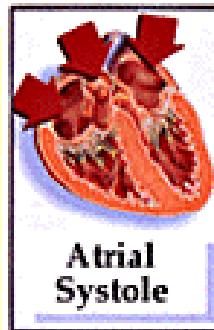
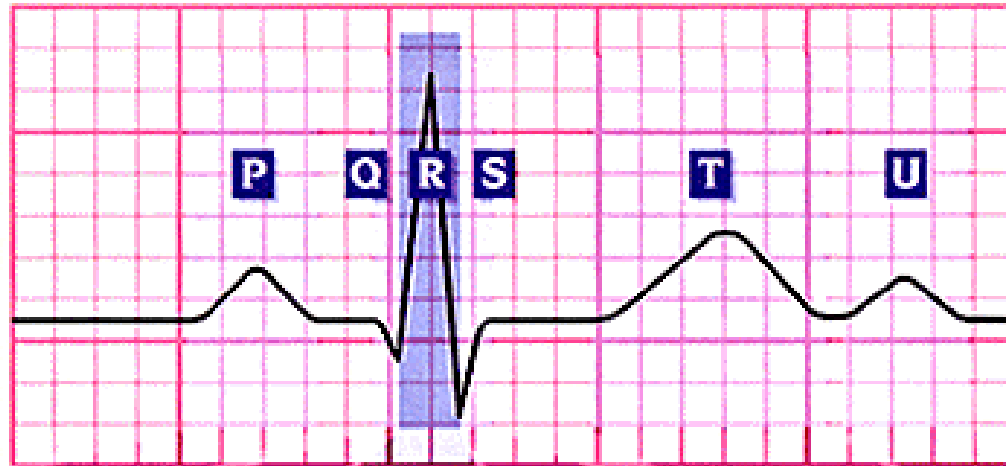


# ECG



Cardiac Conduction System

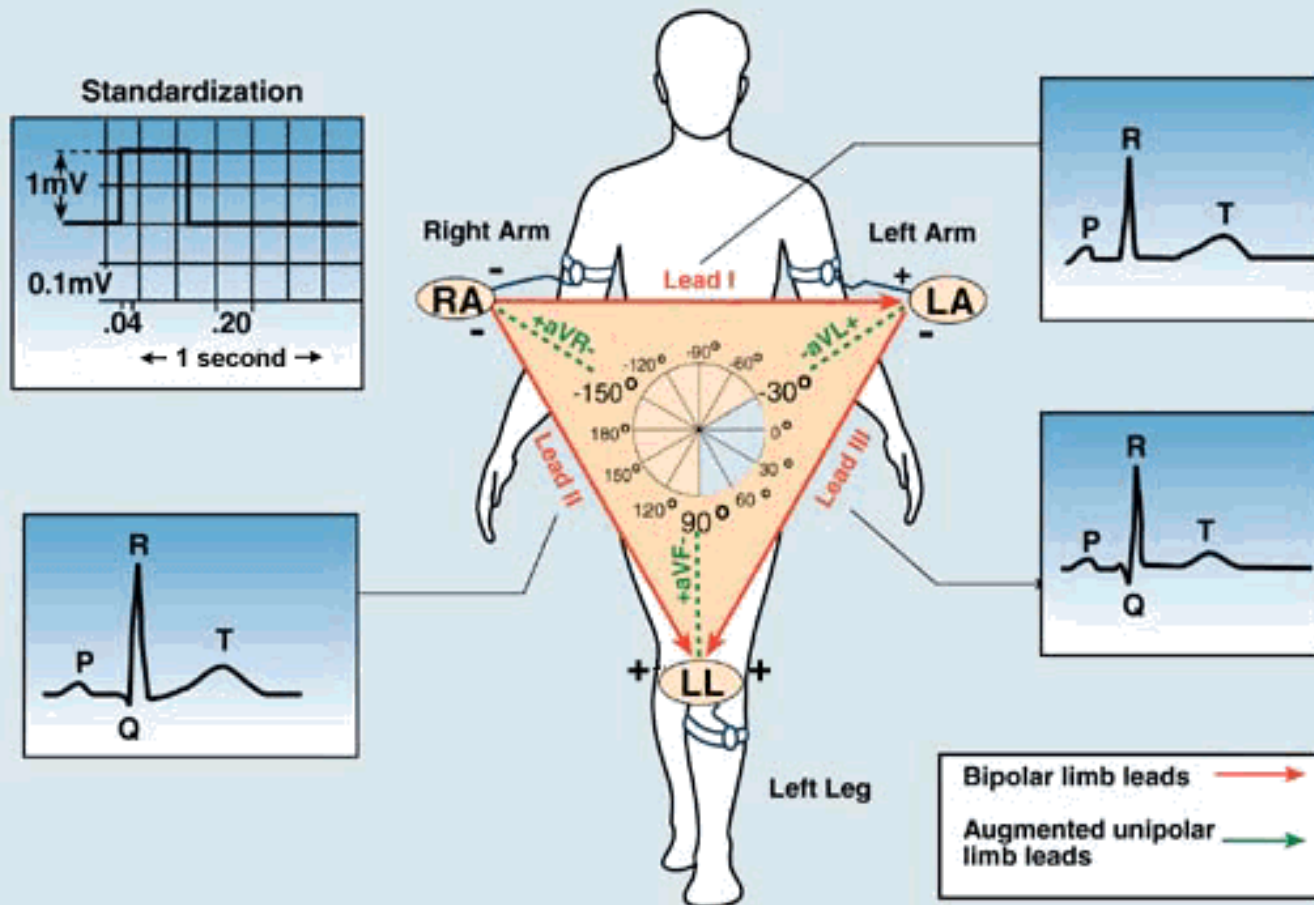
# ECG

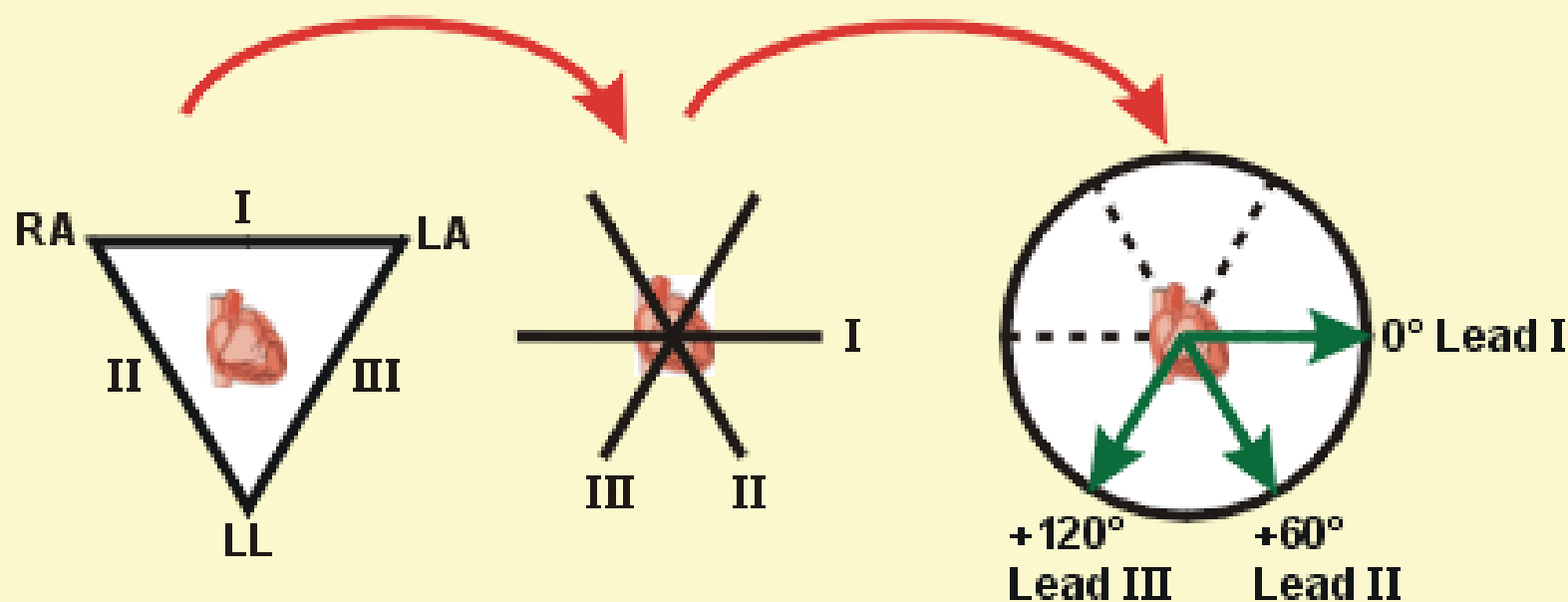
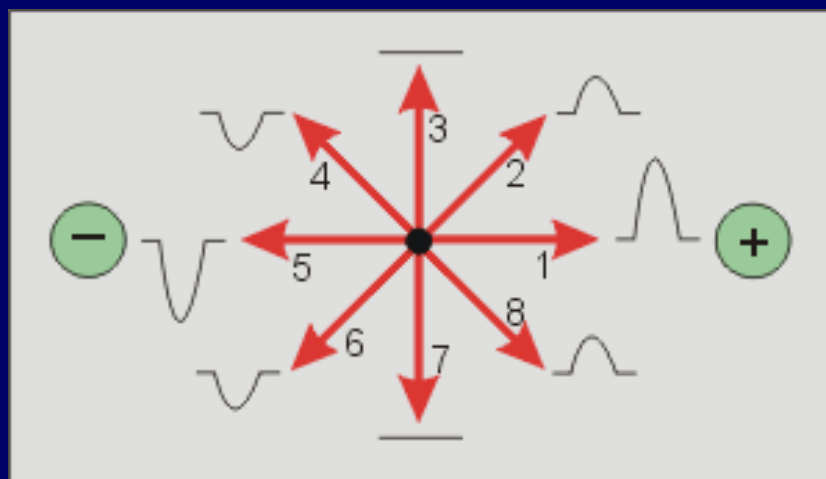


**Electrical and Mechanical Events**

# ECG Leads

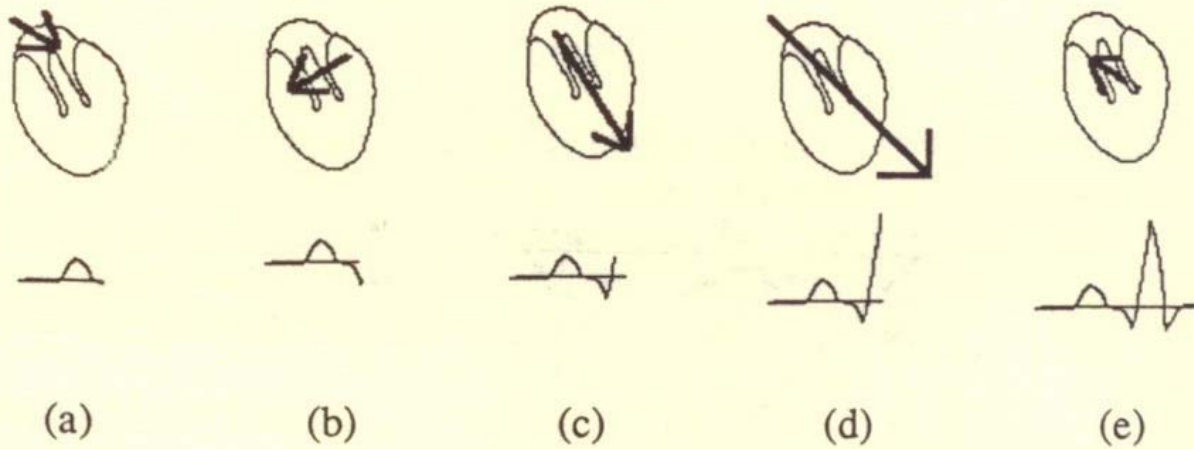
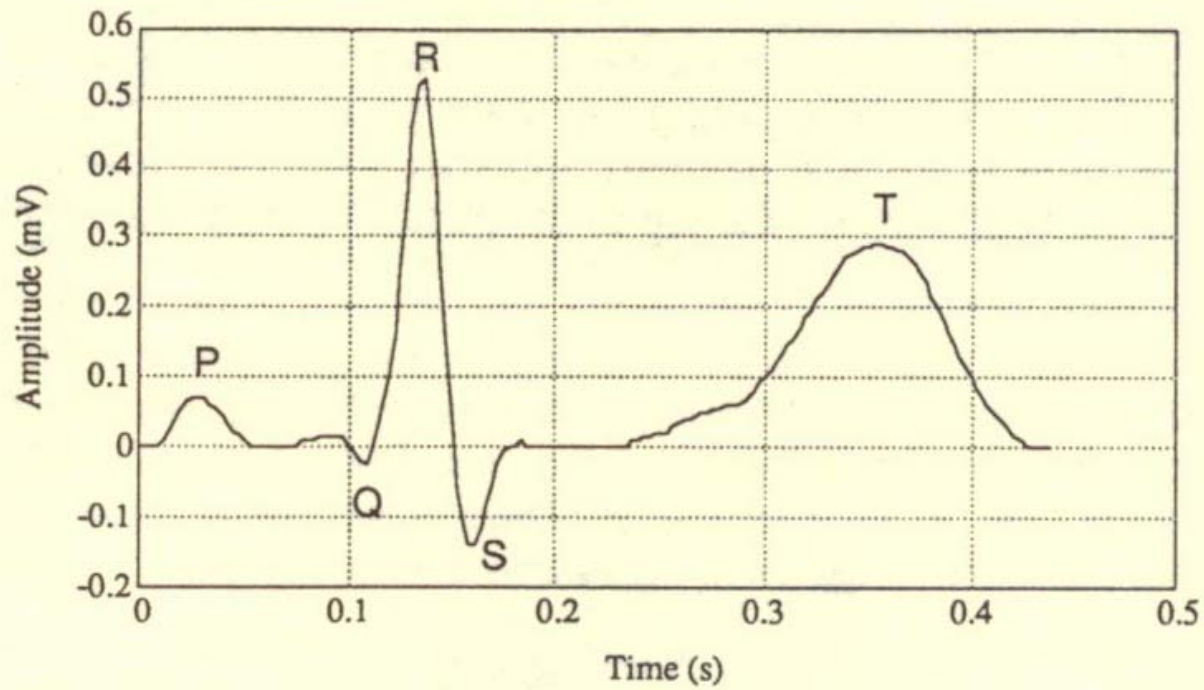
## The Standard Limb Leads



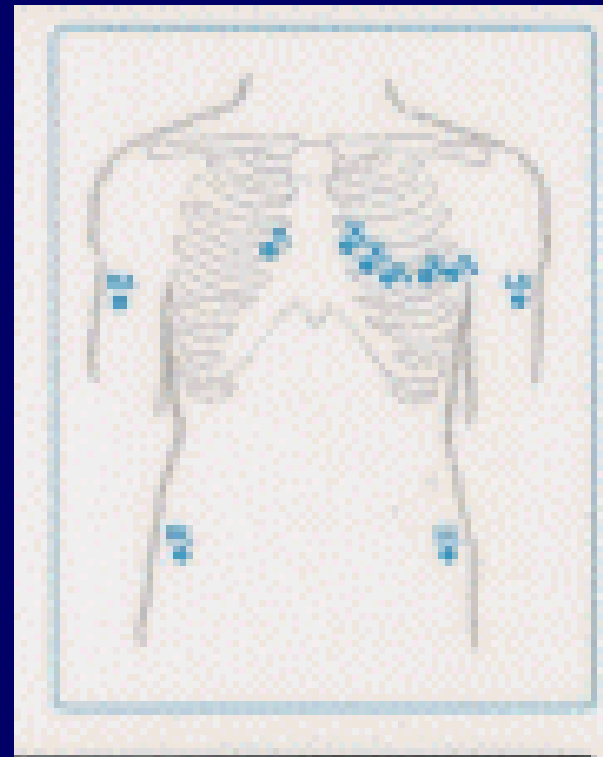
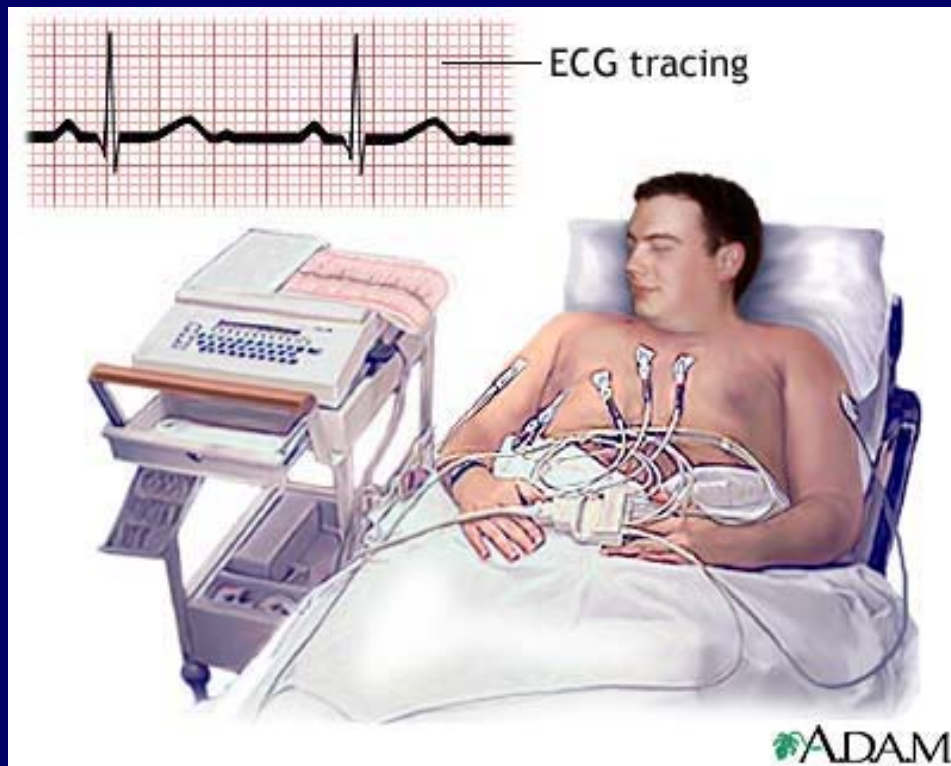


**Einthoven's Triangle**

**Axial Reference System**

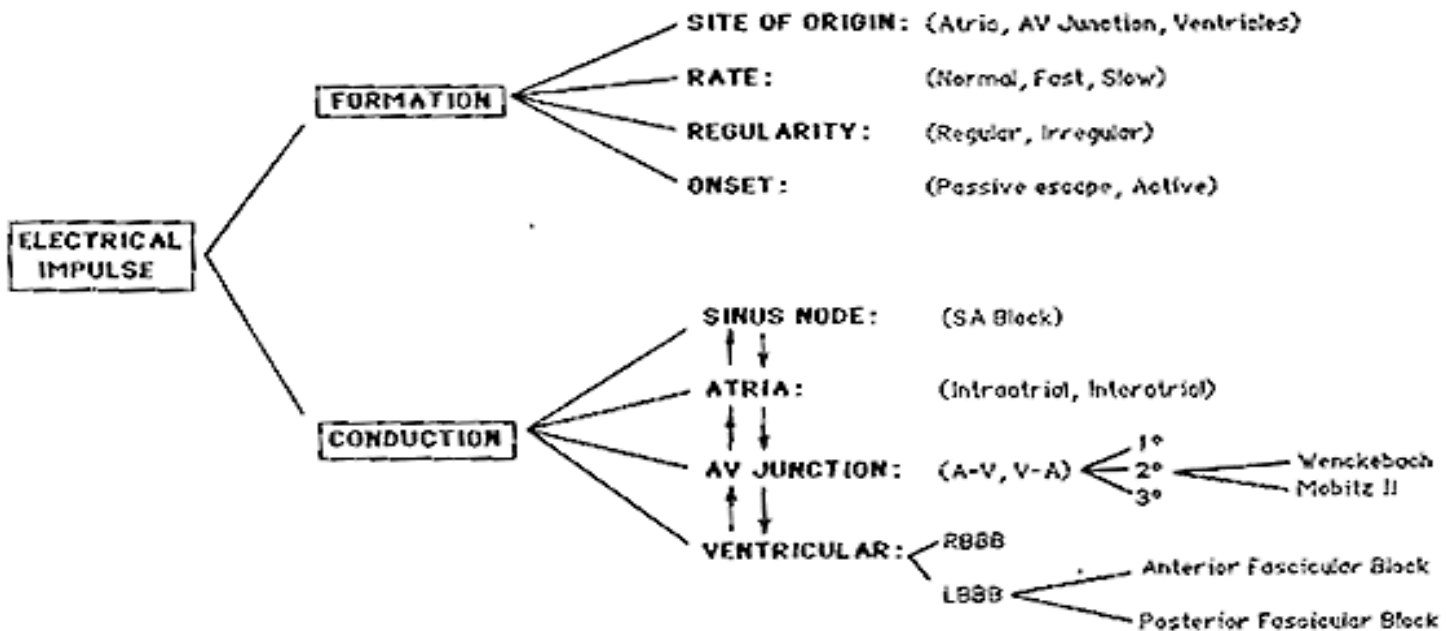


# ECG Leads

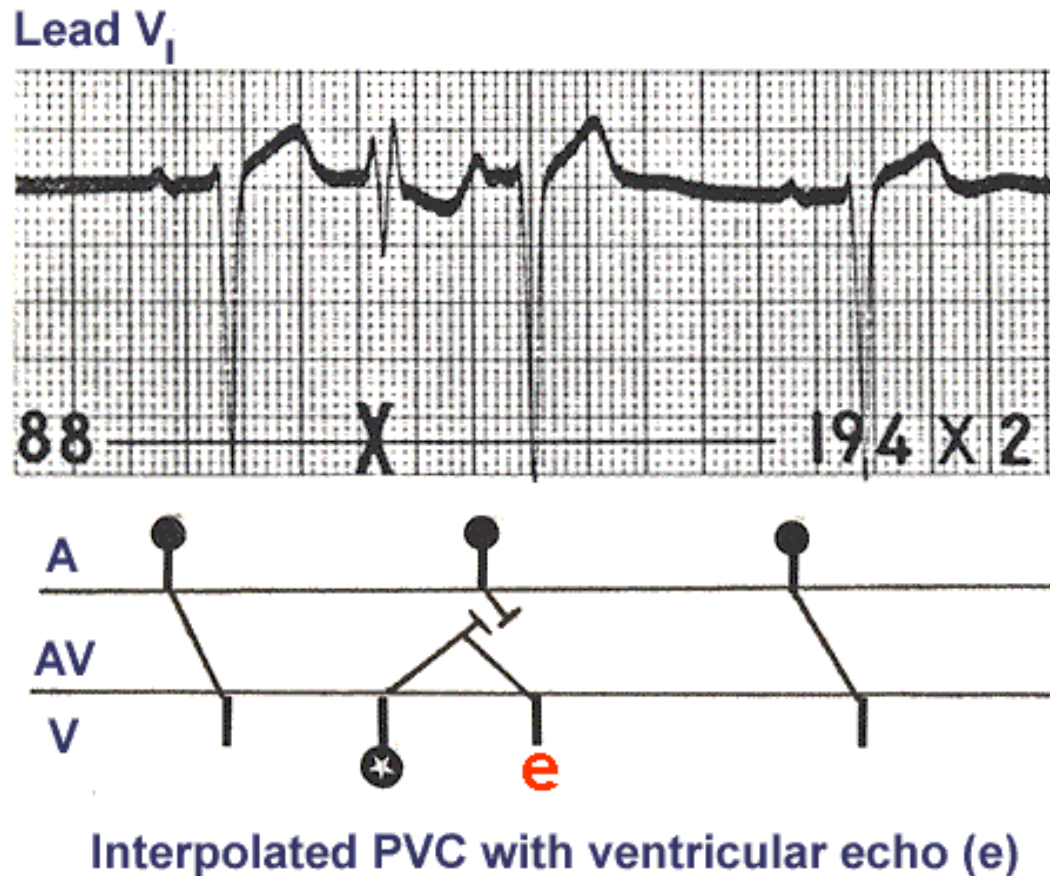


# ECG Diagnosis

## HOW TO THINK ABOUT ARRHYTHMIAS AND CONDUCTION DISTURBANCES



# ECG Diagnosis

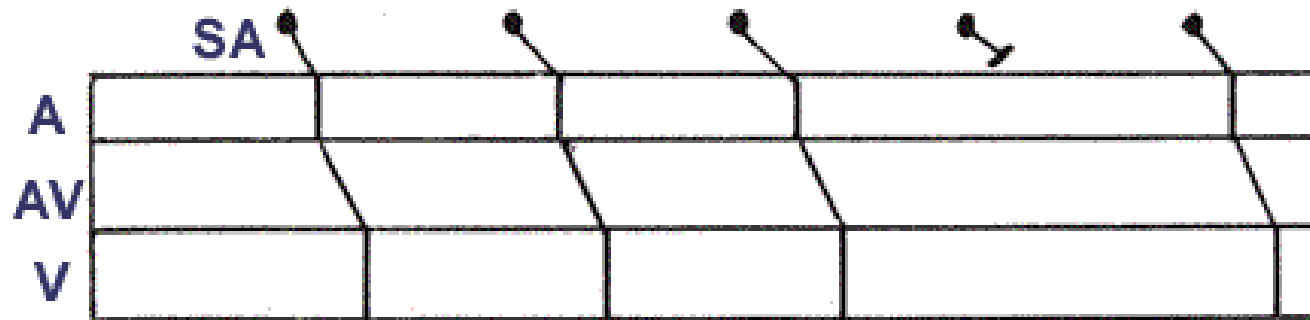


PVC with echo



# ECG Diagnosis

Lead II



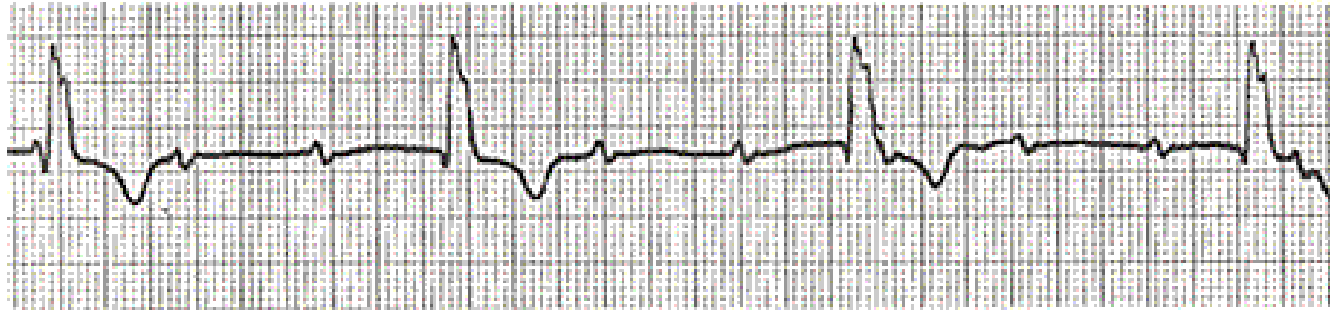
Sino-Atrial Exit Block (type I)

Conduction: SA Block (Type I)

# ECG Diagnosis

Lead V<sub>1</sub>

A



B



Conduction: Complete AV Block

# ECG Diagnosis

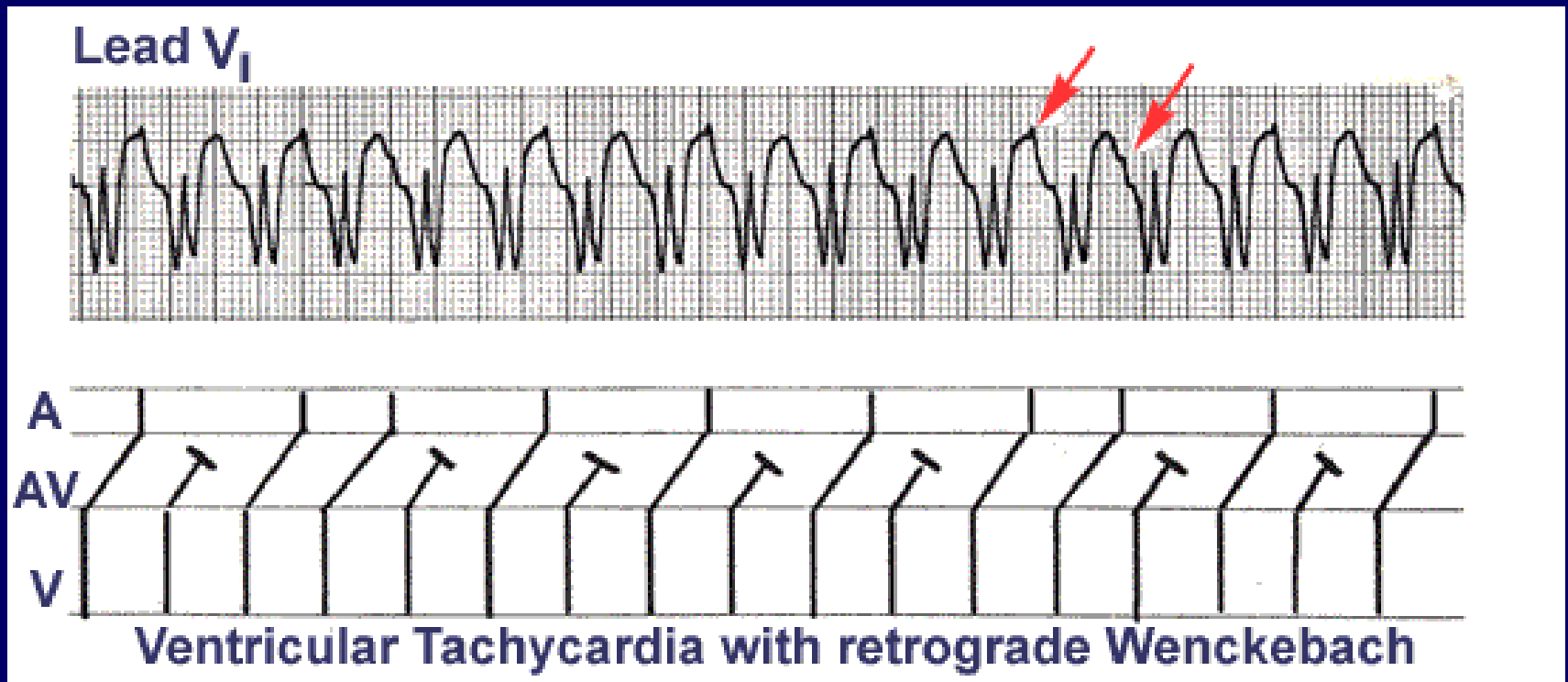
Lead V<sub>1</sub>



Atrial tachycardia with variable AV block

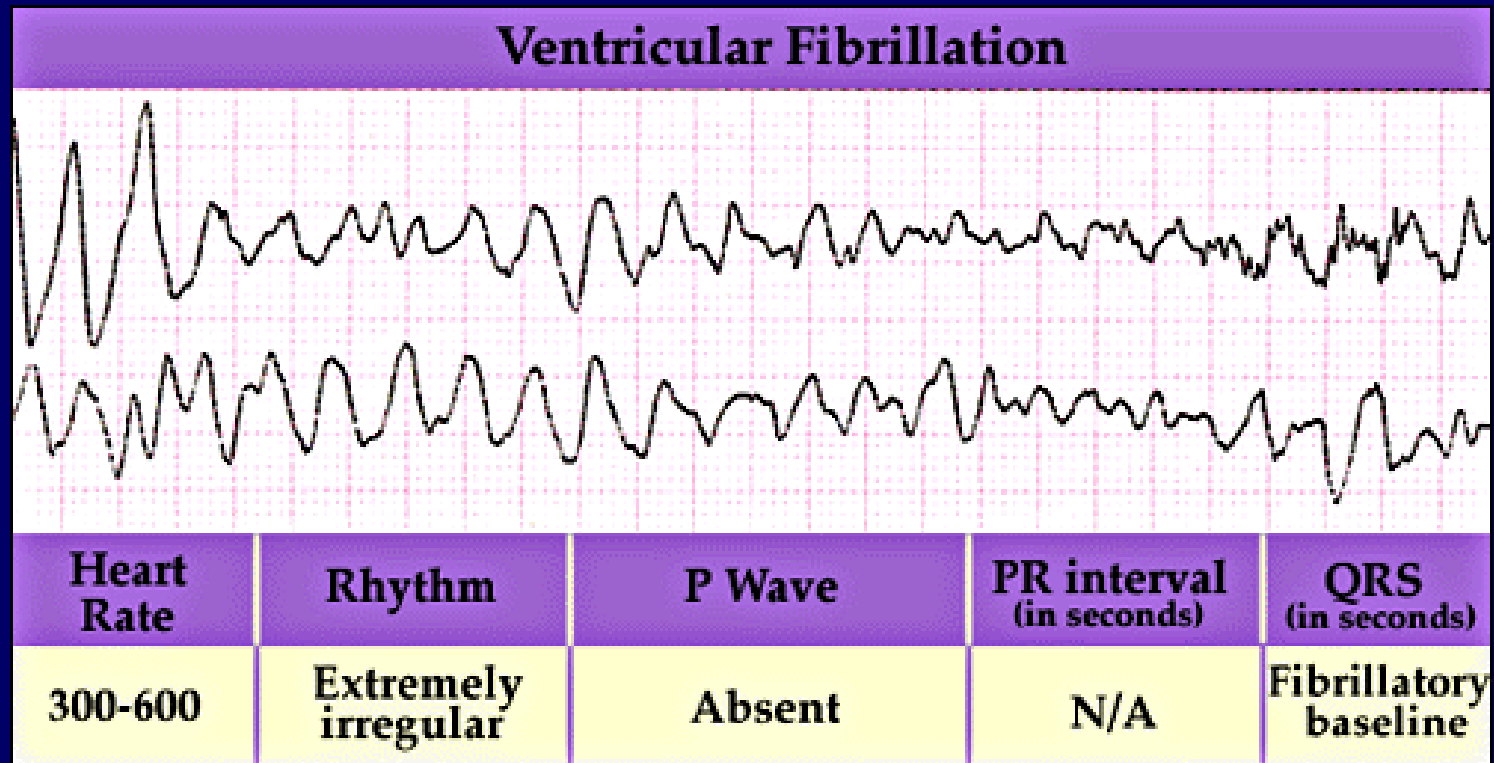
Rate: Atrial Tachycardia (160 bpm)

# ECG Diagnosis



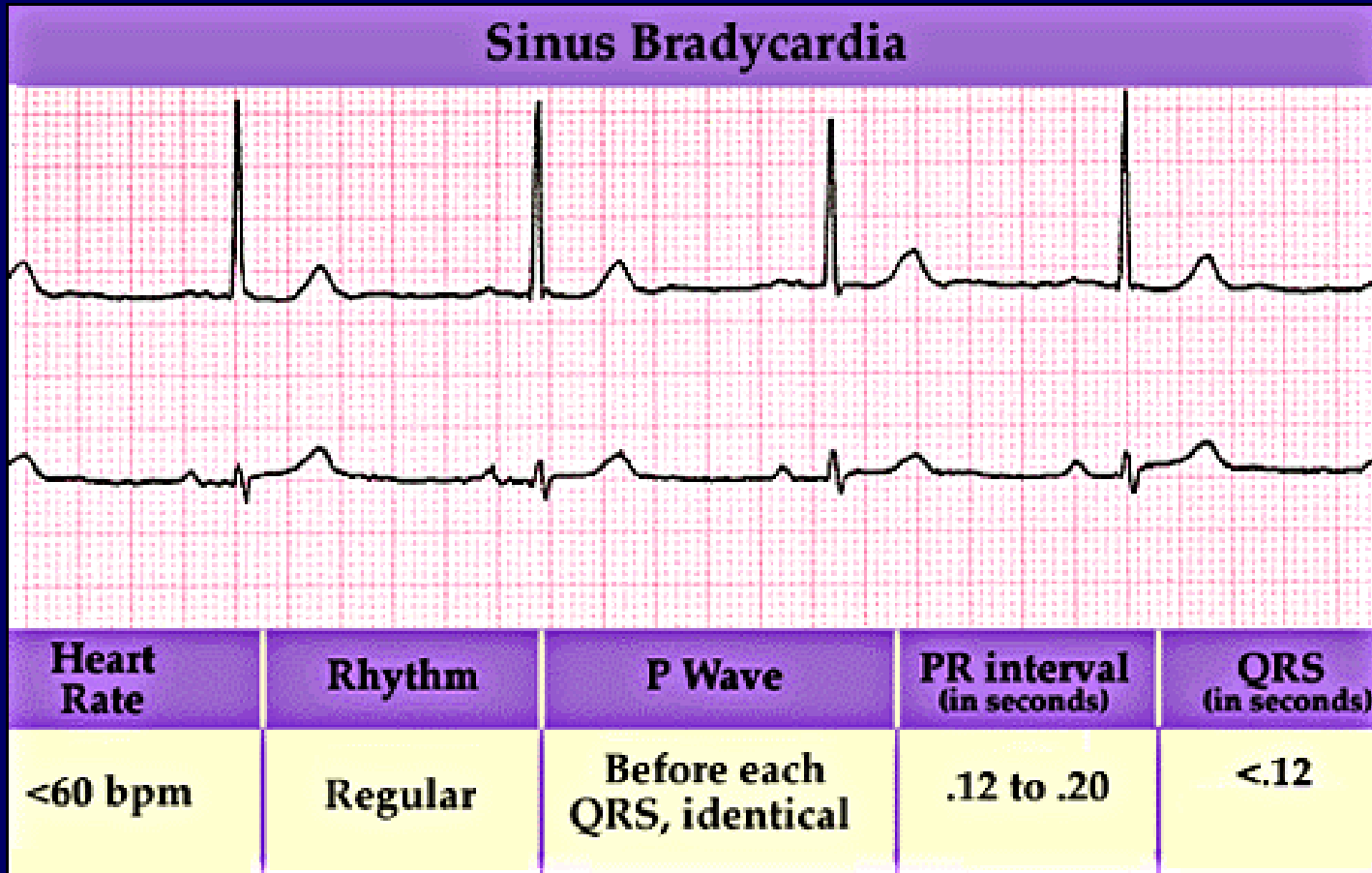
Rate: Ventricular Tachycardia

# ECG Diagnosis



**Rate: Ventricular Fibrillation**

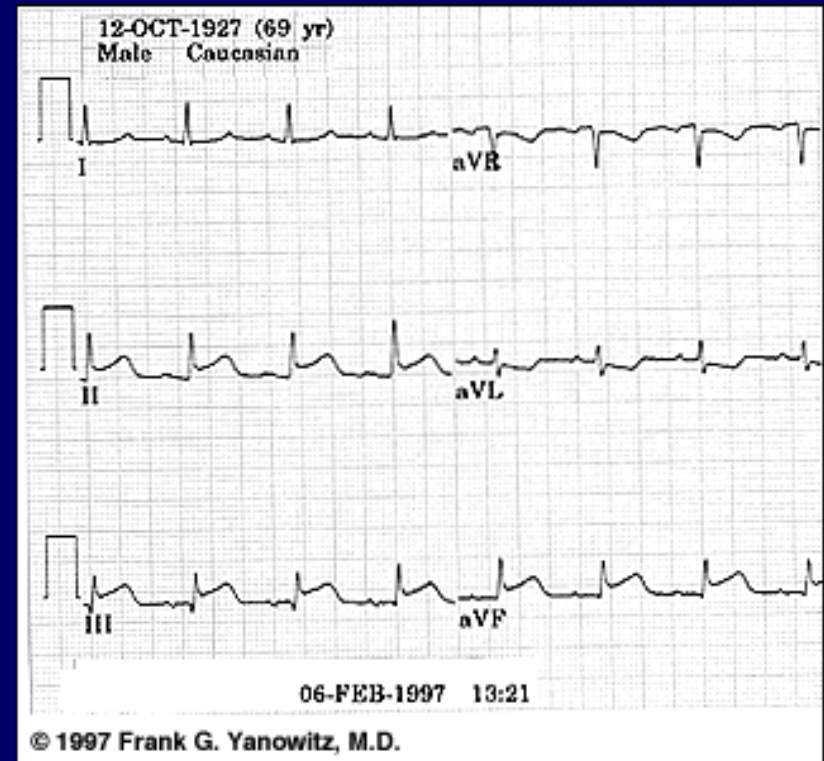
# ECG Diagnosis



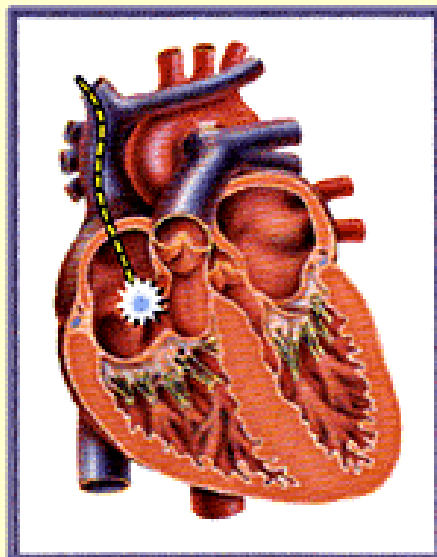
Rate: Sinus Bradycardia

# ECG Diagnosis

- Other abnormalities:
  - Myocardial infarction
  - Atrial/Ventricular enlargement
  - ST segment elevation
  - .....

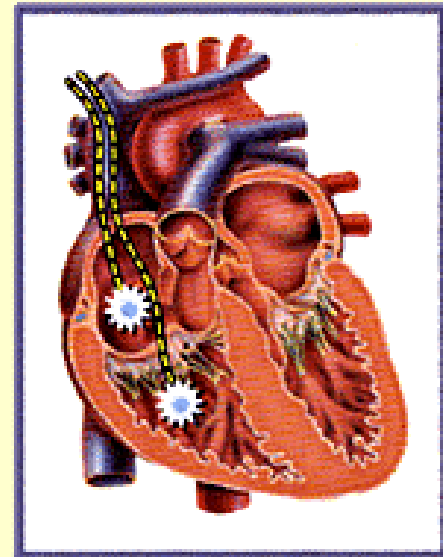
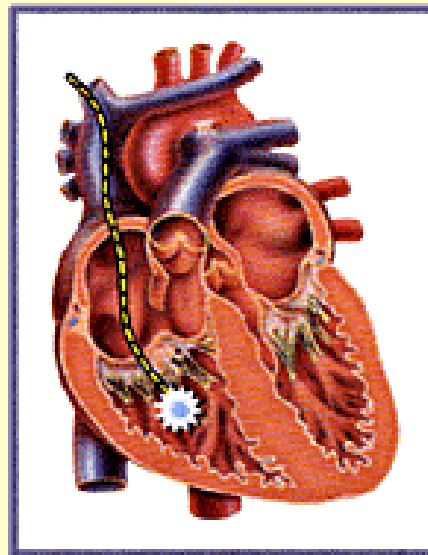


# Pace Makers



**Atrial Pacing**  
The pacing lead is inserted into the atrium to cause atrial depolarization.

**Ventricular Pacing**  
The pacing lead is inserted into the ventricle to cause ventricular depolarization



**A-V Sequential Pacing**  
The pacing leads are inserted into both the atrium and ventricle stimulating at set intervals.

**Pacemaker Lead Wire Replacement**



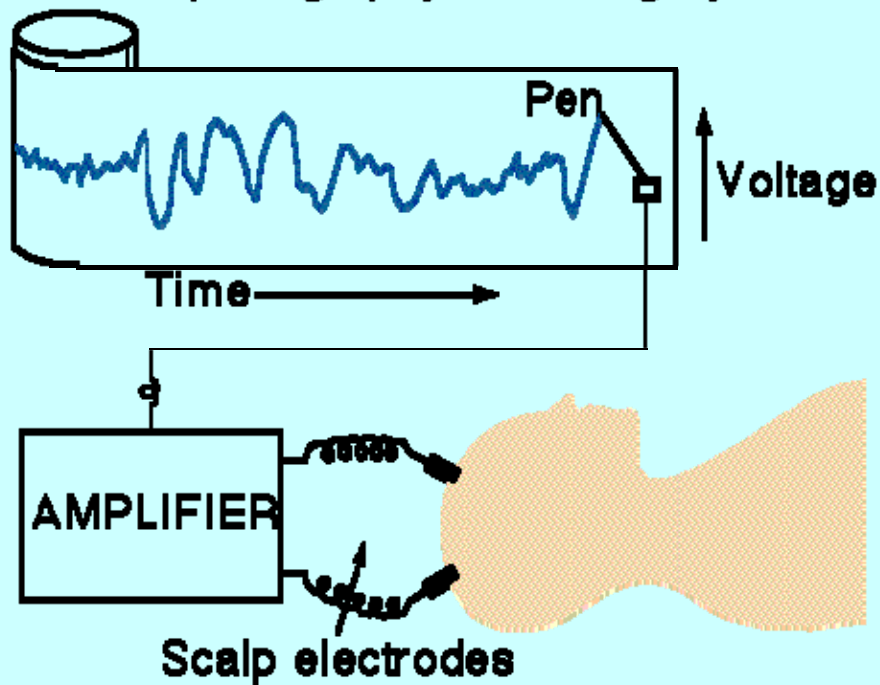
# Electroencephalogram (EEG)

# EEG

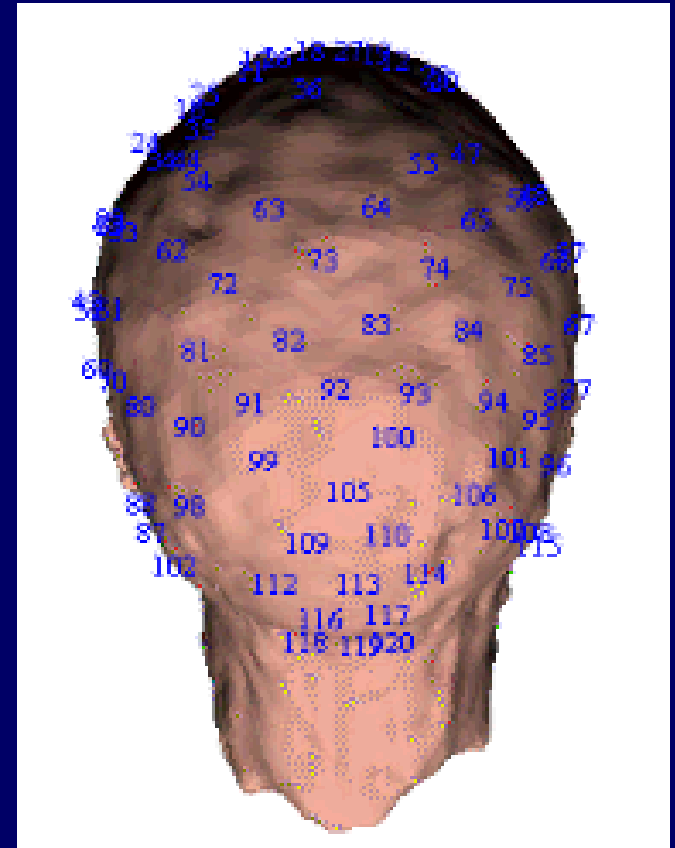
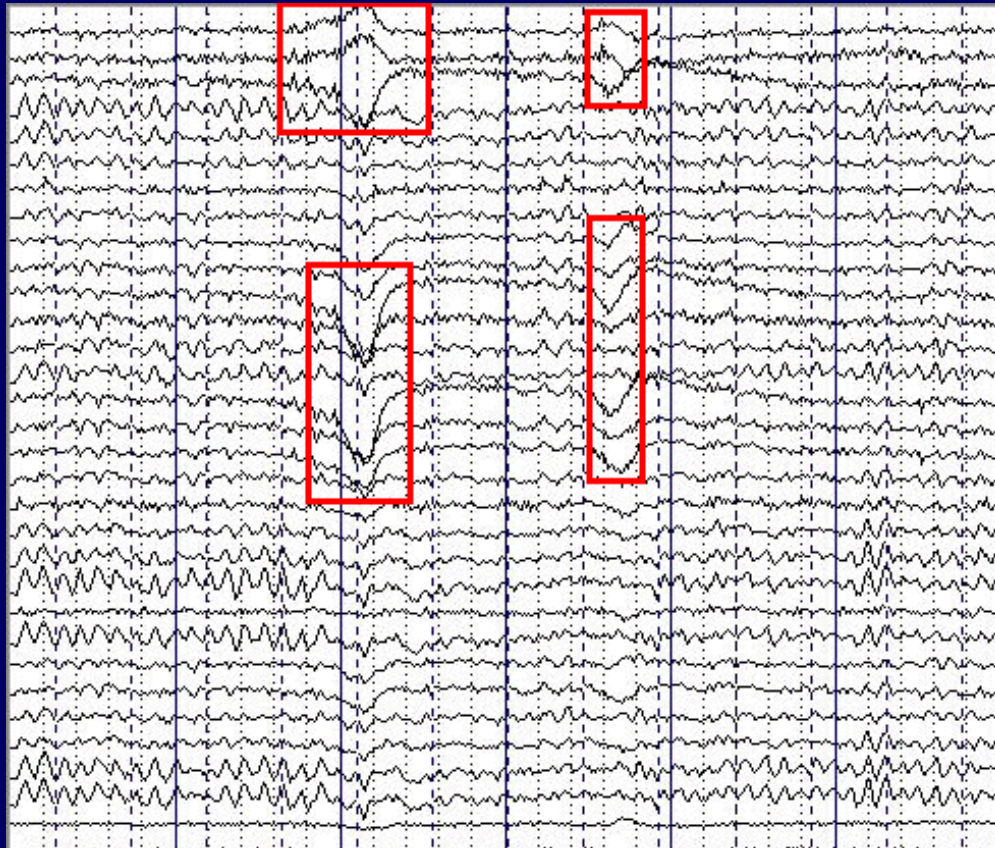
- Electrical potential fluctuations of the brain.
- Under normal circumstances, action potentials in axons are asynchronous.
- If simultaneous stimulation, projection of action potentials are detectable.
- The analysis is based more on frequency than morphology.

# EEG: Instrument

Electroencephalography Recording System



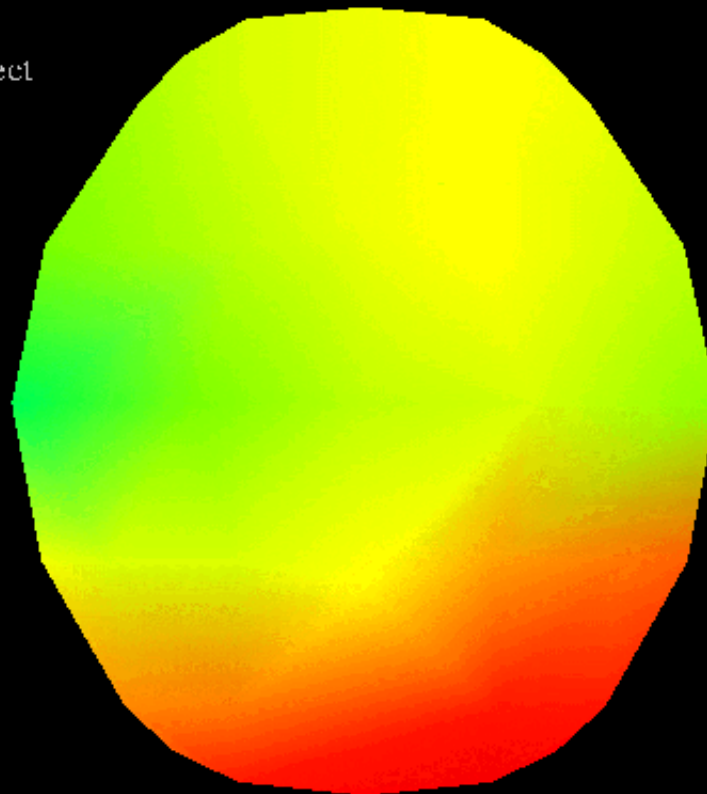
# EEG: Spatial and Temporal Characteristics



# EEG: Presentation

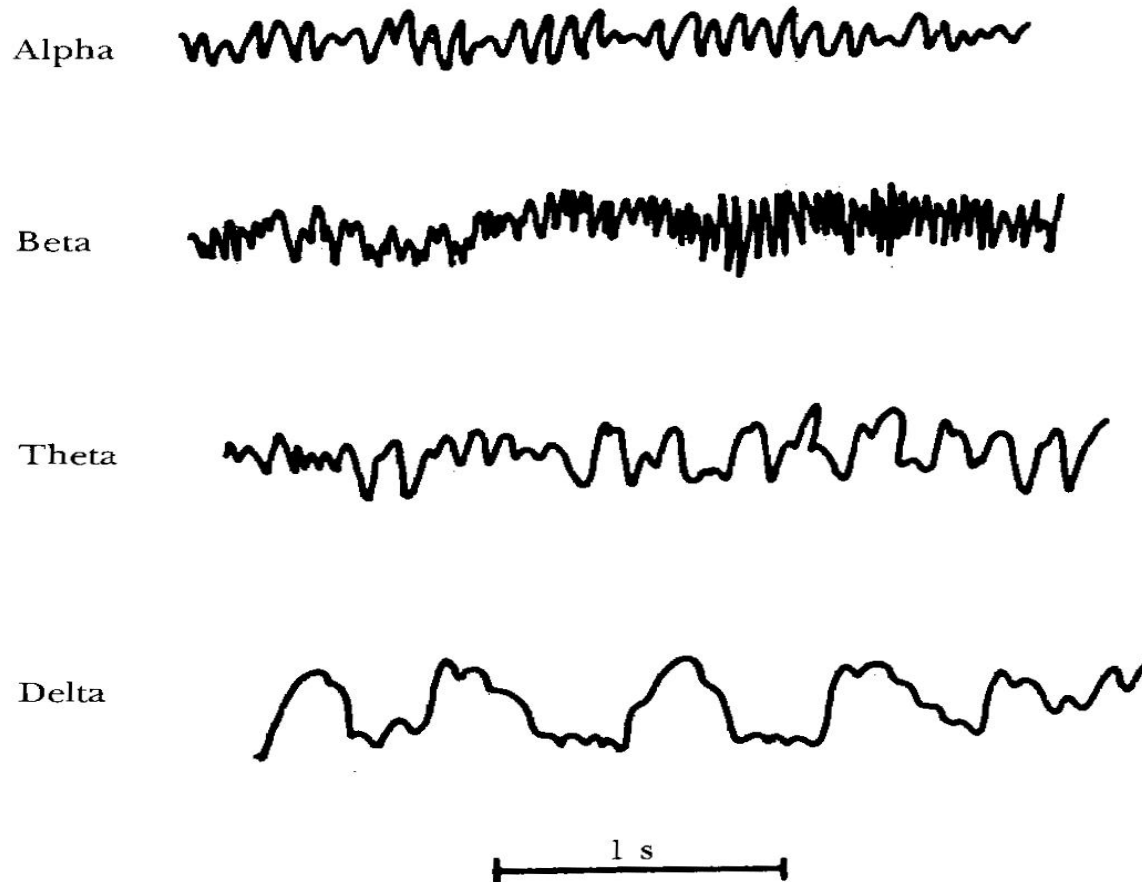
EEG Topographic Map

Young Subject  
Eyes Closed



Voltage

# EEG Classification



# EEG Classification

- Alpha:
  - 8 to 13Hz.
  - Normal persons are awake in a resting state.
  - Alpha waves disappear in sleep.
- Beta:
  - 14 to 30Hz.
  - May go up to 50Hz in intense mental activity.
  - Beta I waves: frequency about twice that of the alpha waves and are influenced in a similar way as the alpha waves.
  - Beta II waves appear during intense activation of the central nervous system and during tension.

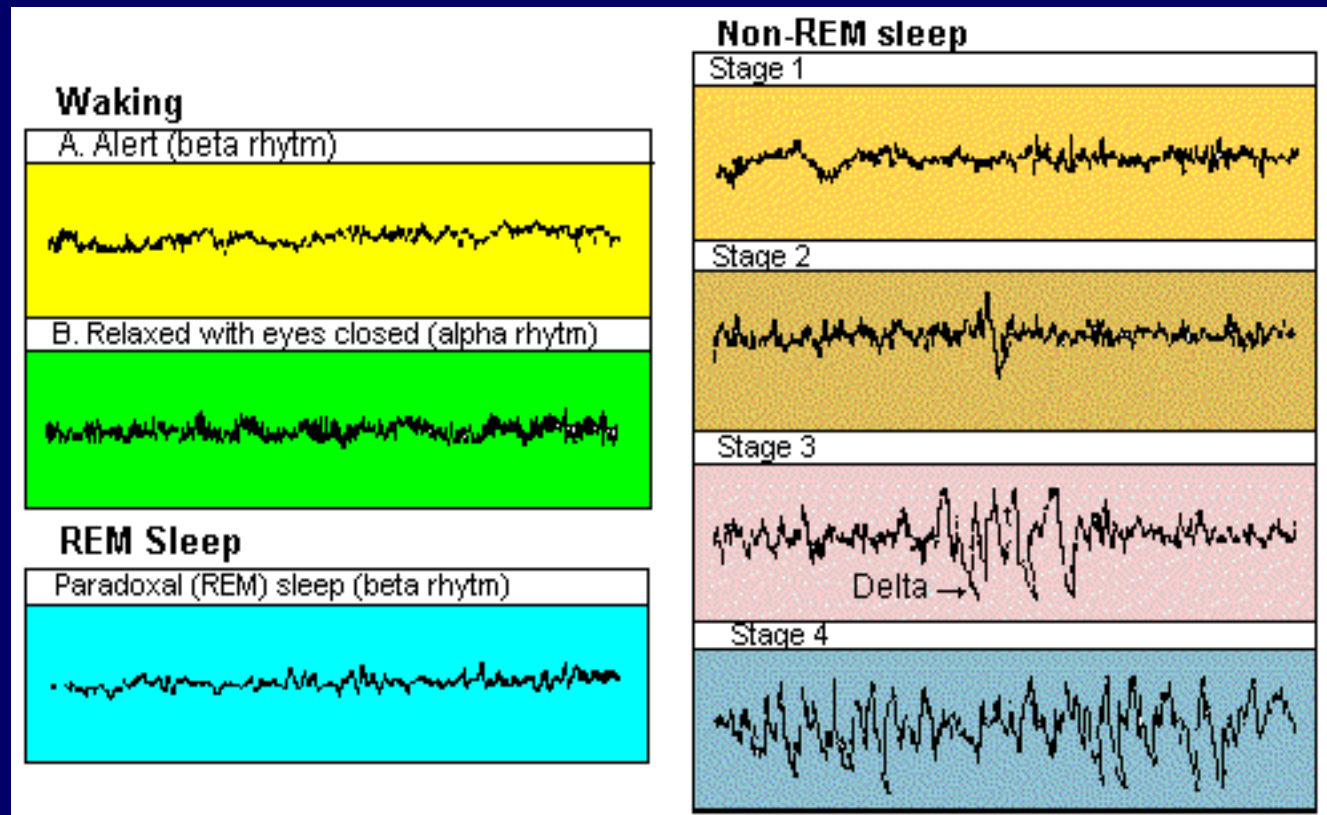
# EEG Classification

- Theta waves:
  - 4 to 7Hz.
  - During emotional stress.
- Delta waves
  - Below 3.5Hz.
  - Deep sleep or in serious organic brain disease.



# EEG Applications

- Epilepsy.
- Dream:



# Other Biomedical Signals

- Electrical:
  - Electroneurogram (ENG)
  - Electromyogram (EMG)
  - Electroretinogram (ERG)
  - Electrogastrogram (EGG).

# Other Non-Electrical Biomedical Signals

- Circulatory system
  - Blood pressure
  - Heart sound
  - Blood flow velocity
  - Blood flow volume

# Other Non-Electrical Biomedical Signals

- Respiratory system
  - Respiratory pressure
  - Gas-flow rate
  - Lung volume
  - Gas concentration

# Applications of Signal Processing Techniques

# Sampling

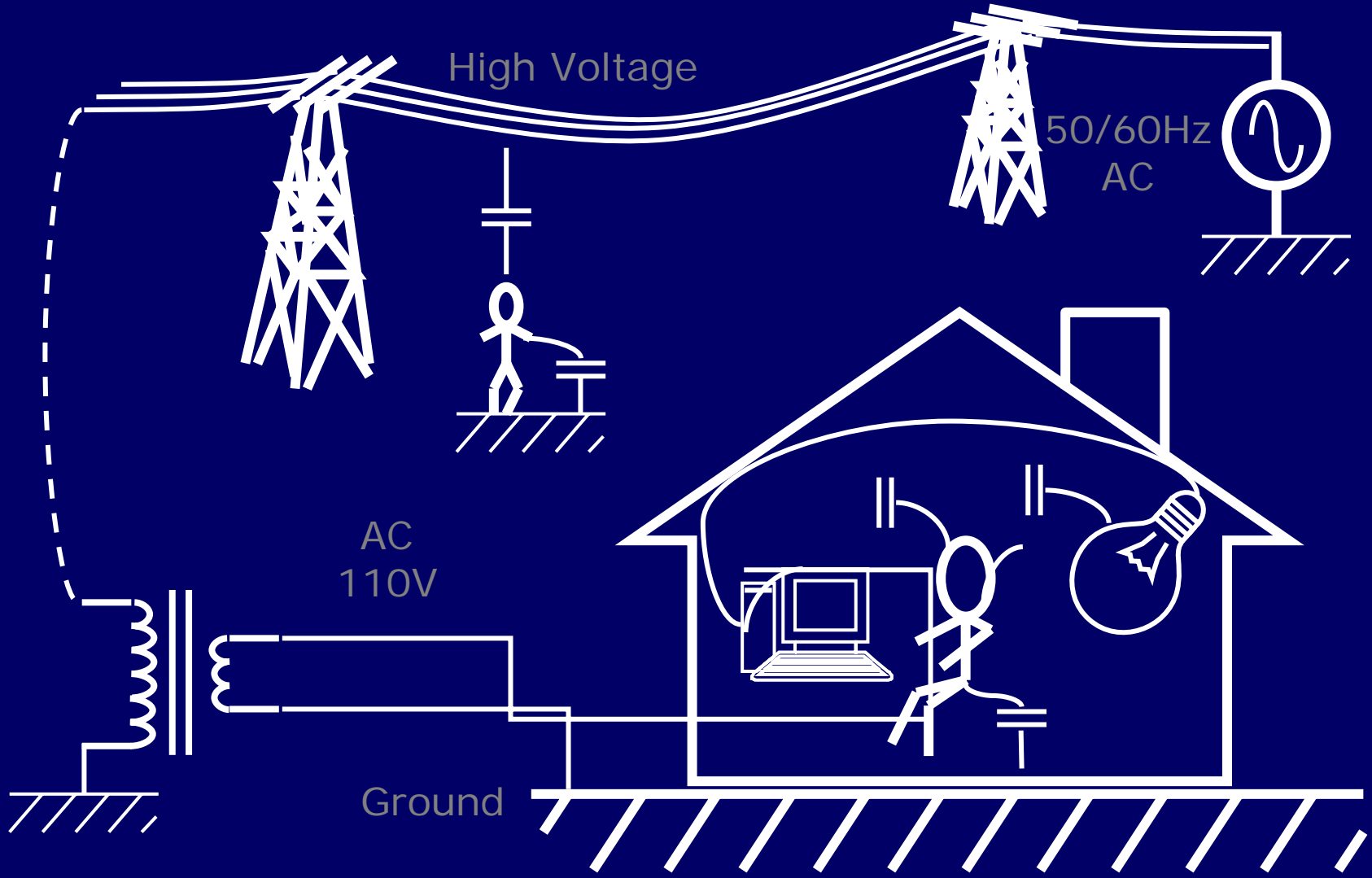
- Digital analysis and presentation of biomedical signals.
- Sampling requirements.
  - Low frequencies.
  - Frequency ranges of different physiological signals may be overlapping.
  - Electronic noise and interference from other physiological signals.
  - Very weak (maybe  $\mu\text{V}$  level), the pre-amp circuit is often very challenging.

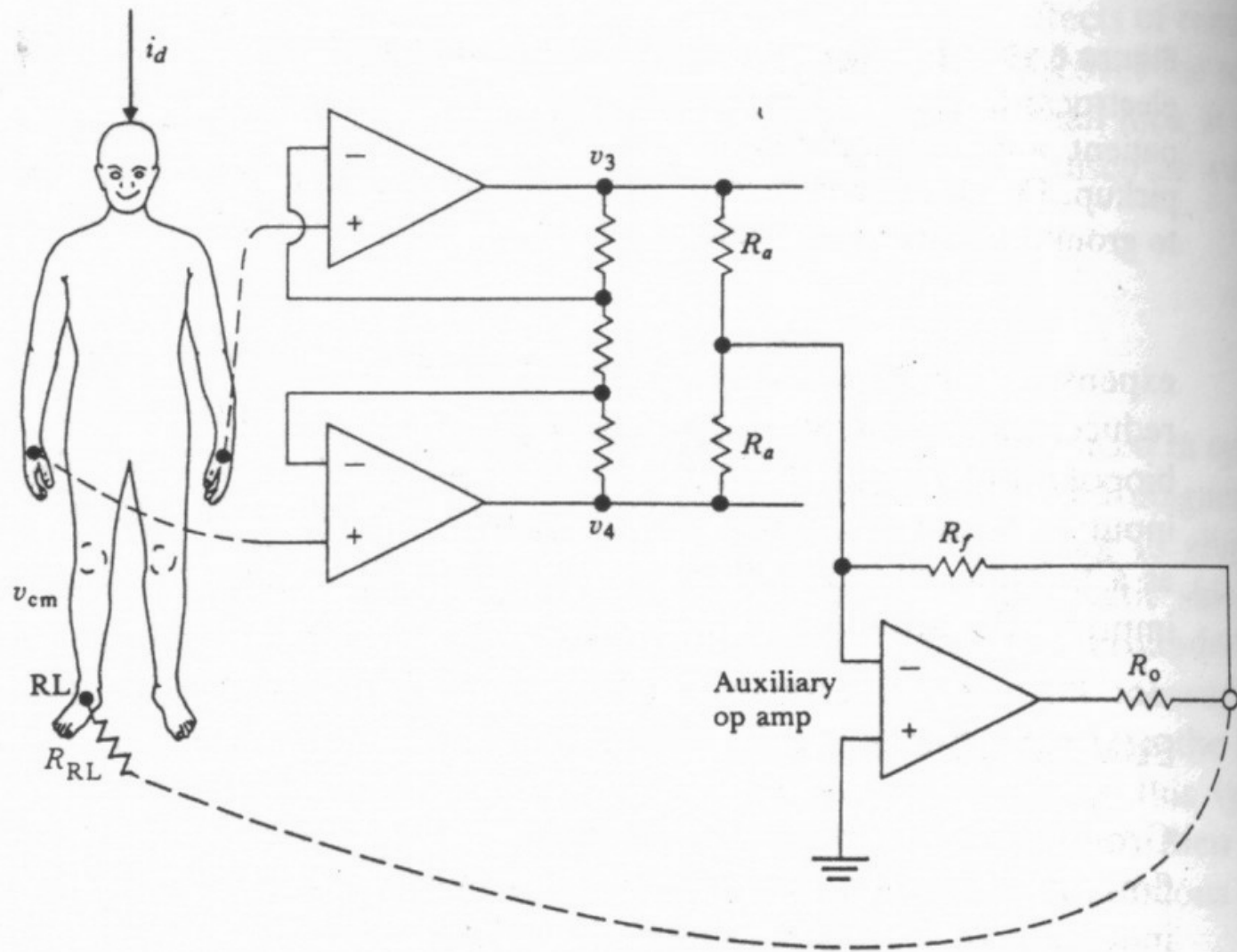
# Filtering

- Digital filters are used to keep the in-band signals and to reject out-of-band noise.
- Low-pass, band-pass, high-pass and band-reject.
- Similar to those of other applications.

# Noise Sources of ECG



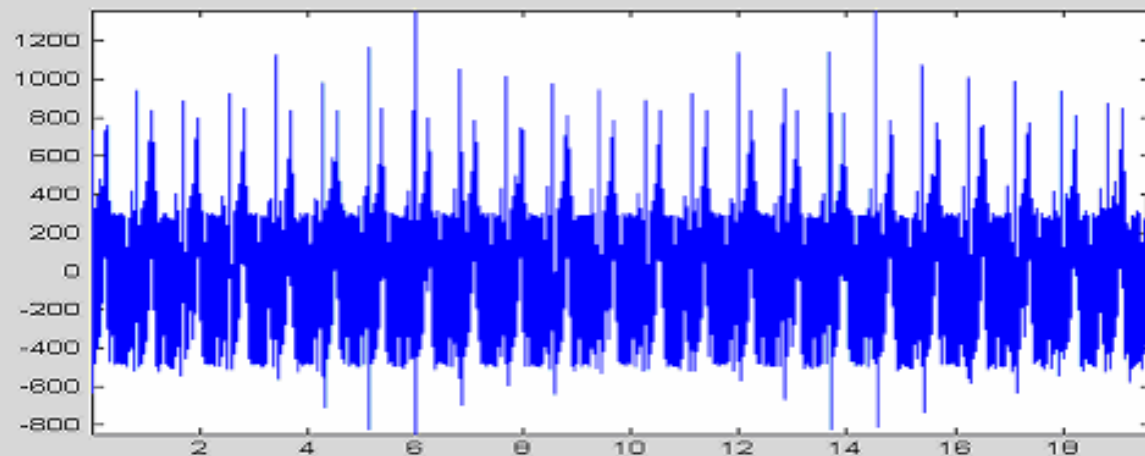
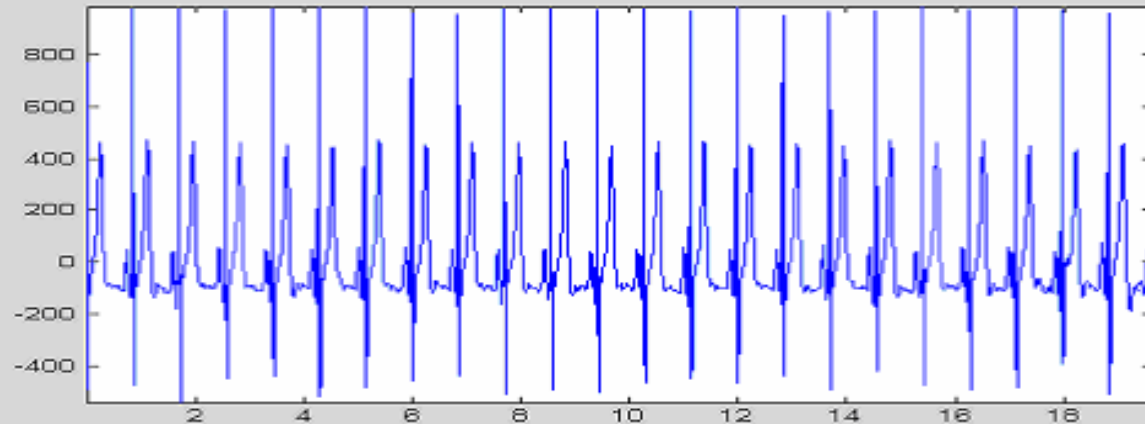




# Noise Sources

- Inherent
- Instrumentation
- Environment
- From the body
- ...

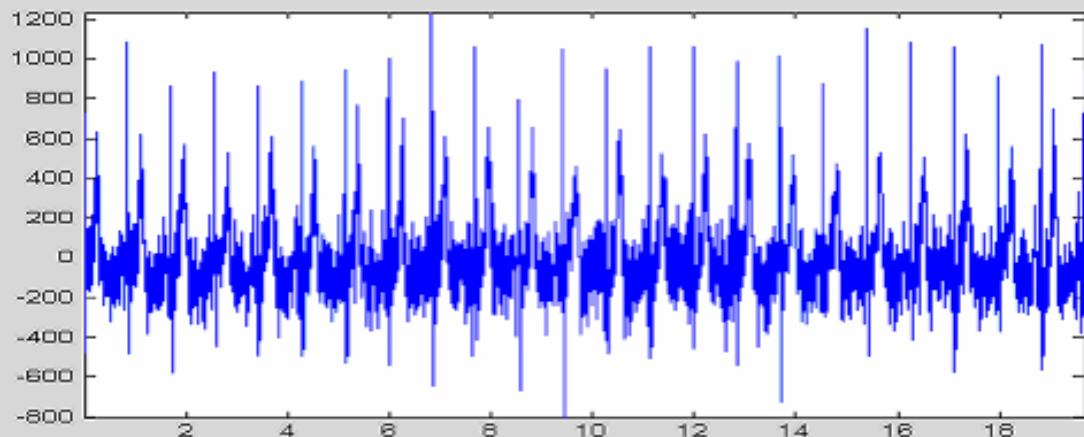
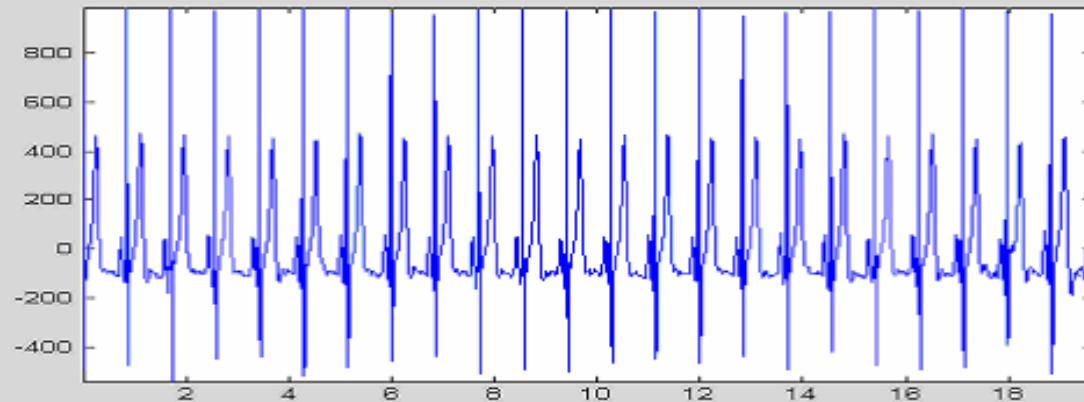
# Ideal Signal Vs. Signal with Powerline Noise



# Ideal Signal Vs. Signal with Powerline Noise

- Powerline interference consists of 60Hz tone with random initial phase.
- It can be modeled as sinusoids and its combinations.
- The characteristics of this noise are generally consistent for a given measurement situation and, once set, will not change during a detector evaluation. Its typical SNR is in the order of 3dB.

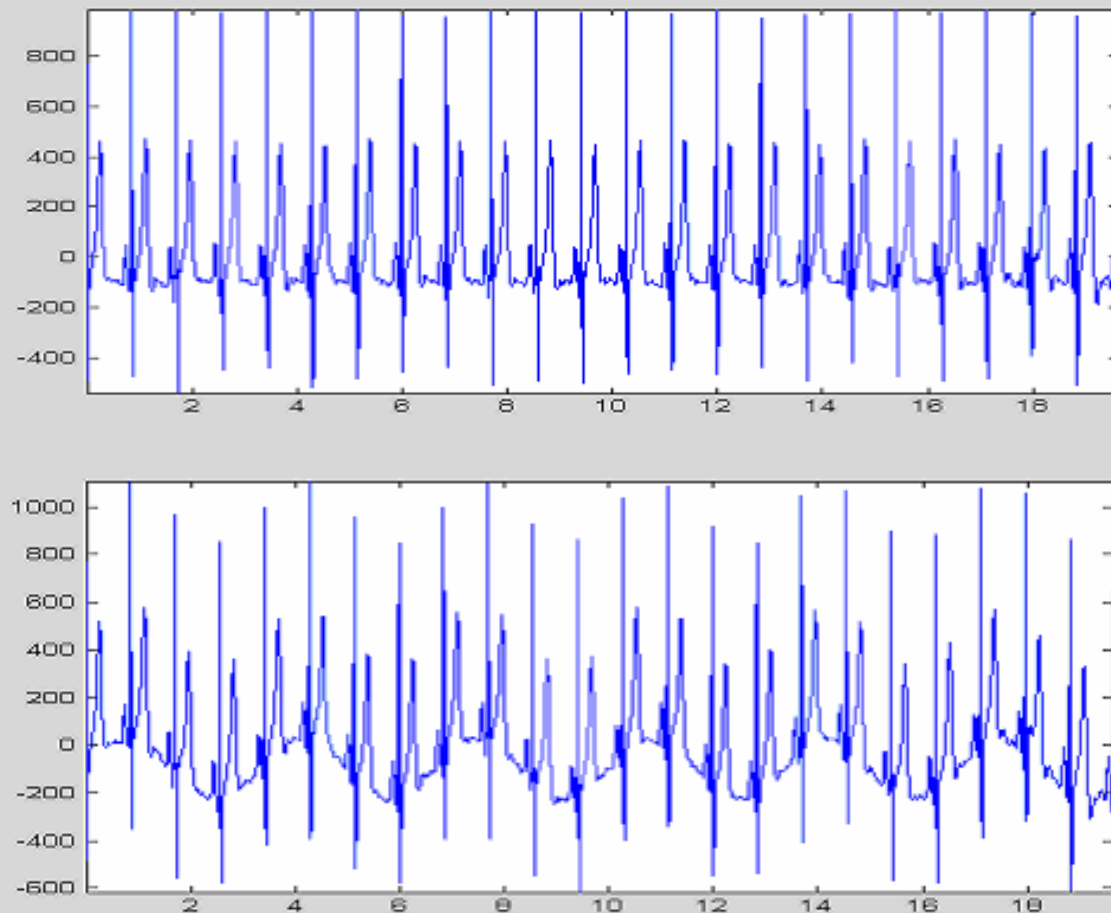
# Ideal Signal Vs. Signal with Electromyographic Noise



# Ideal Signal Vs. Signal with Electromyographic Noise

- EMG noise is caused by muscular contractions, which generate millivolt-level potentials.
- It is assumed to be zero mean Gaussian noise. The standard deviation determines the SNR, whose typical value is in the order of 18dB.

# Ideal Signal Vs. Signal with Respirational Noise

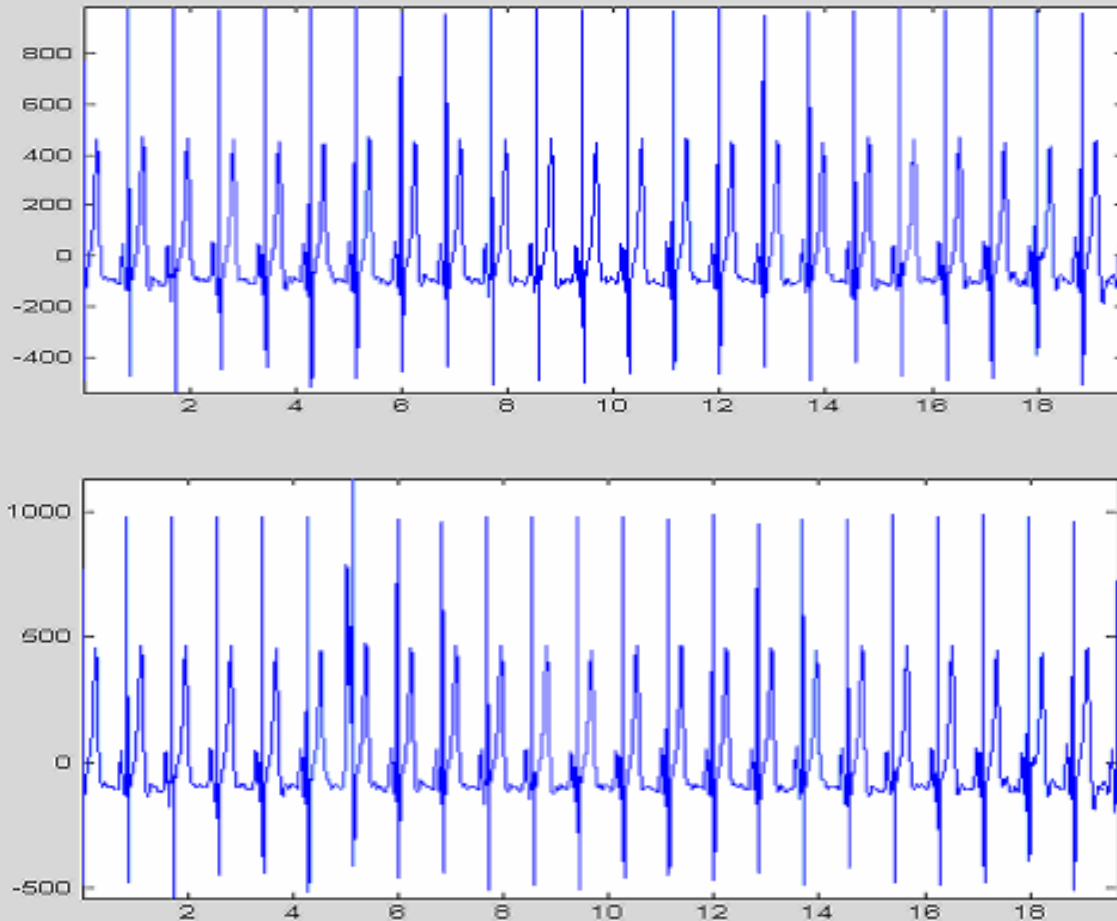




# Ideal Signal Vs. Signal with Respirational Noise

- Respiration noise considers both the sinusoidal drift of the baseline and the ECG sinusoidal amplitude modulation.
- The drift can be represented as a sinusoidal component at the frequency of respiration added to the ECG signal.
- The amplitude variation is about 15 percent of peak-to-peak ECG amplitude. It is simulated with a sinusoid of 0.3Hz frequency with typical SNR 32dB.
- The modulation is another choice of representing respiration noise. It can be simulated with 0.3Hz sinusoid of 12dB SNR.

# Ideal Signal Vs. Signal with Motion Artifacts



# Ideal Signal Vs. Signal with Motion Artifacts

- Motion artifact is caused by displacements between electrodes and skin due to patients' slow movement.
- It is simulated with an exponential function that decays with time.
- Typically the duration is 0.16 second and the amplitude is almost as large as the peak-to-peak amplitude.
- The phase is random with a uniform distribution.

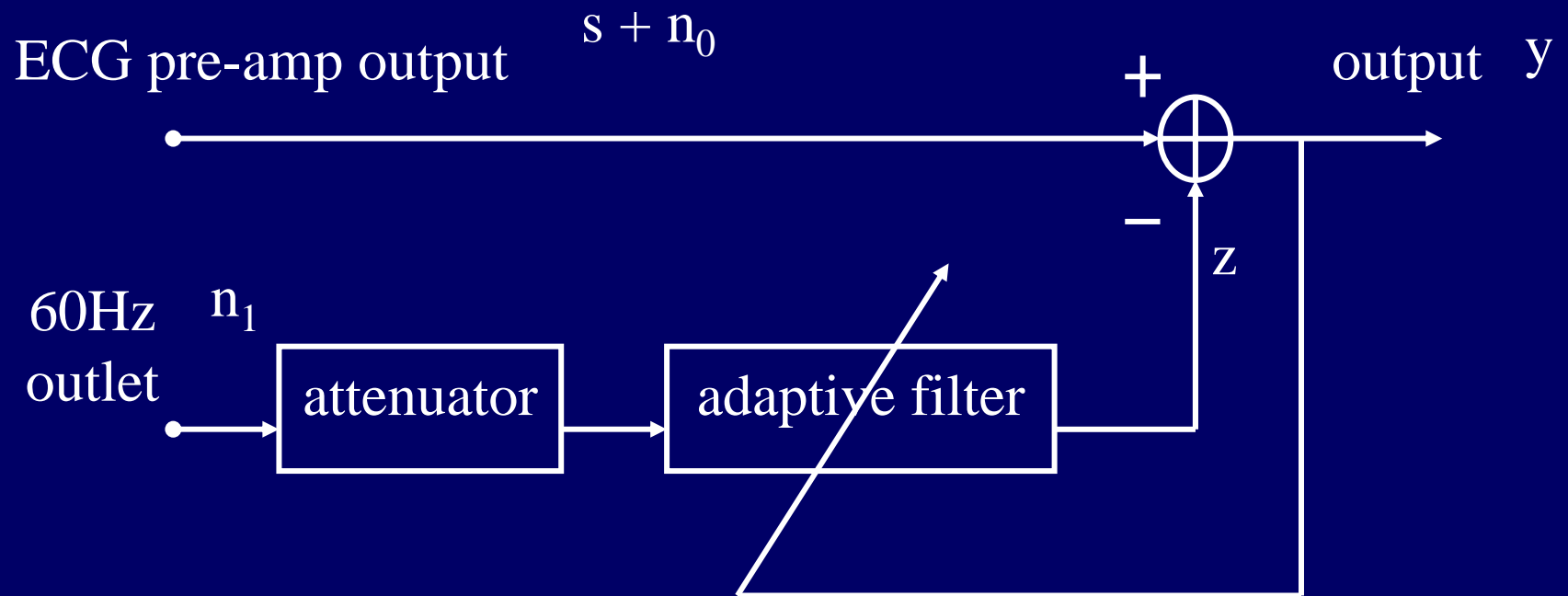
# Noise Removal

- The four types of noises are mostly sinusoidal or Gaussian. The sinusoidal noises are usually removed with a notch filter. Other distortions are zeroed out using the moving average.

# Adaptive Noise Cancellation

- Noise from power line (60Hz noise).
- The noise is also in the desired frequency range of several biomedical signals (e.g., ECG), notch filter is required.
- Adaptive filtering: The amplitude and exact frequency of the noise may change.

# Adaptive Filter



# Adaptive Filter

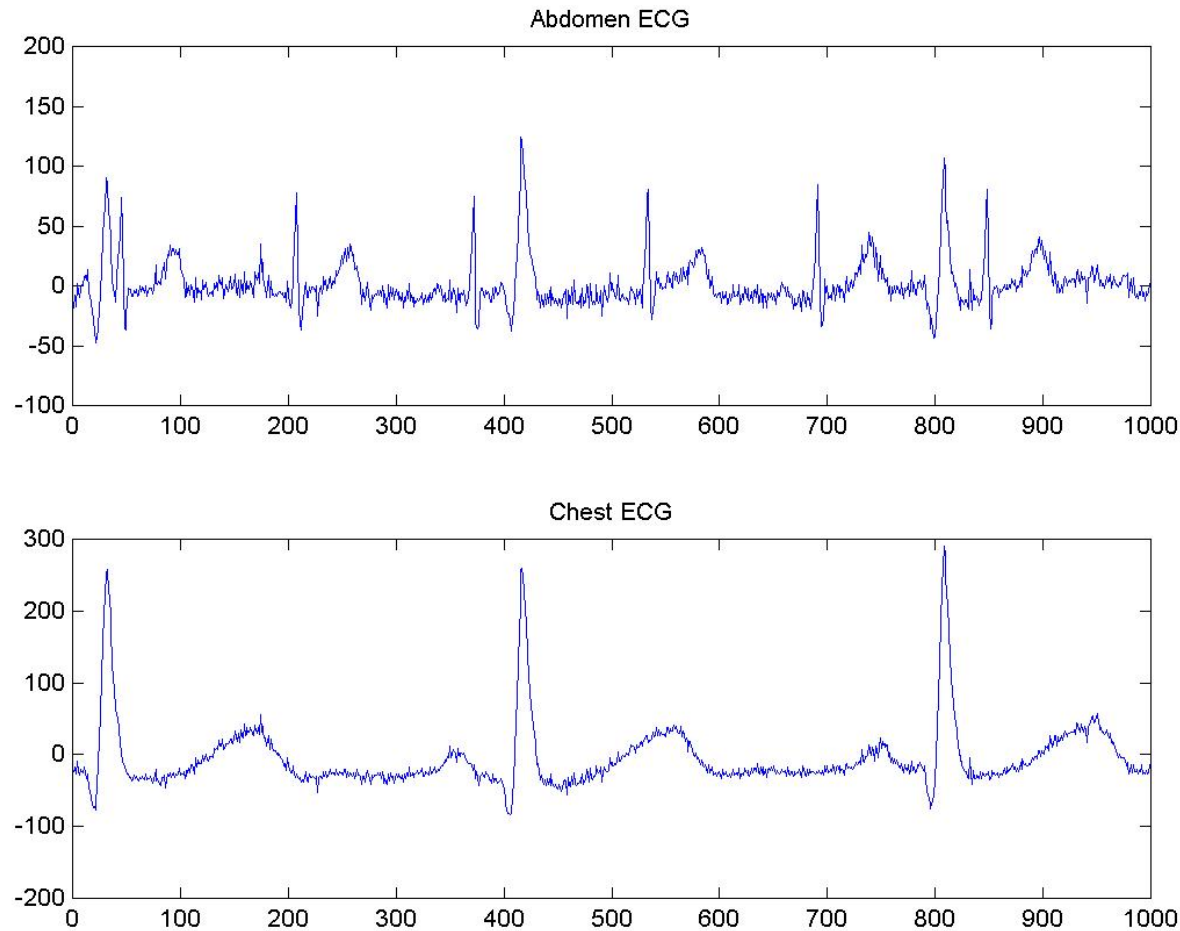
$$y(nT) = s(nT) + n_0(nT) - z(nT)$$

$$y^2 = s^2 + (n_0 - z)^2 + 2s(n_0 - z)$$

$$E[y^2] = E[s^2] + E[(n_0 - z)^2] + 2E[s(n_0 - z)] = E[s^2] + E[(n_0 - z)^2]$$

$$\min E[y^2] = E[s^2] + \min E[(n_0 - z)^2]$$

# Adaptive Filtering for Fetal ECG





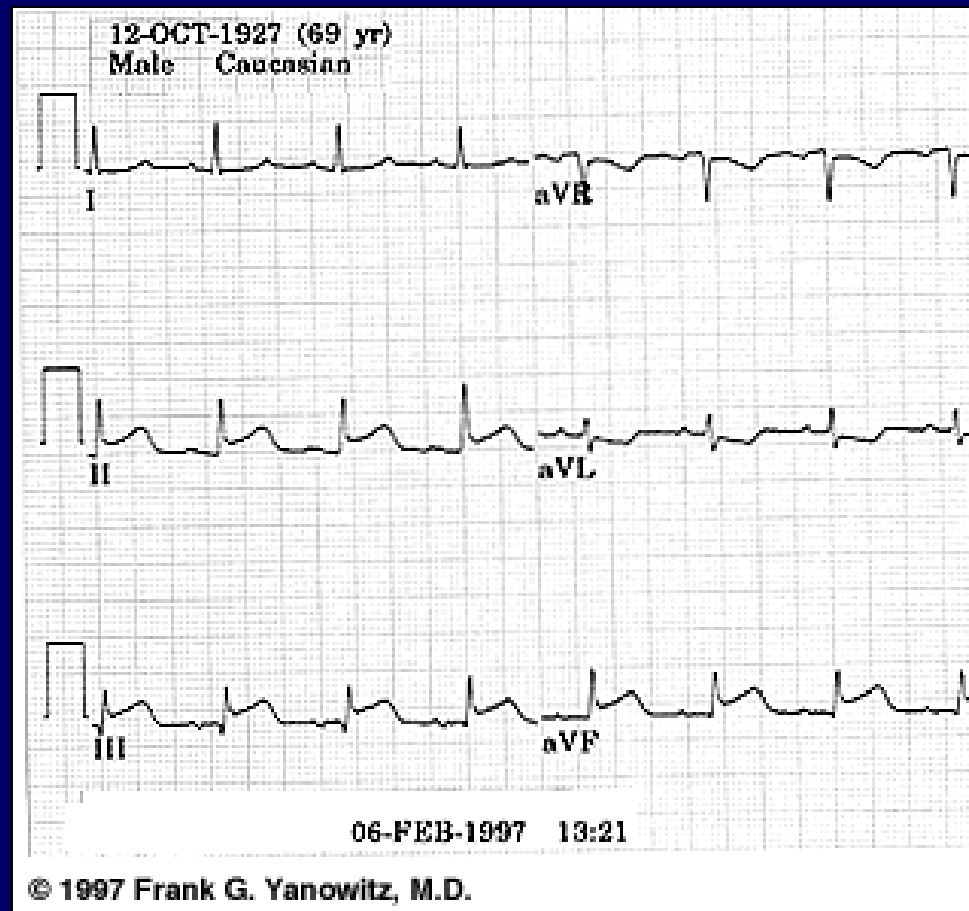
# Pattern Recognition

- Abnormal physiological signals vs. the normal counterparts.
- An average of several known normal waveforms can be used as a template.
- The new waveforms are detected, segmented and compared to the template.
- Correlation coefficient can be used to quantify the similarity.

$$\rho = \frac{\sum_{i=1}^N (T_i - \mu_T)(X_i - \mu_X)}{\sqrt{\sum_{i=1}^N (T_i - \mu_T)^2} \sqrt{\sum_{i=1}^N (X_i - \mu_X)^2}}$$

# Pattern Recognition

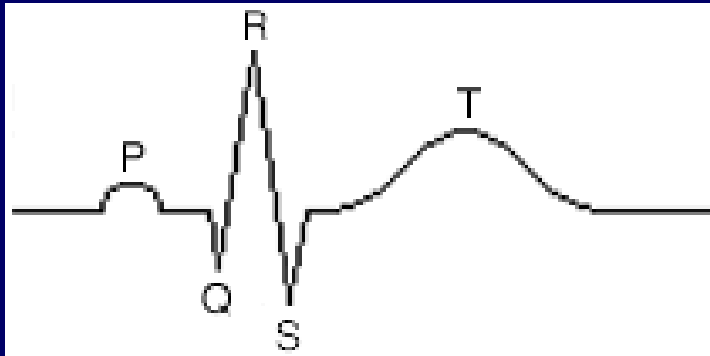
Ex. ECG



# Data Compression

- For large amount of data (e.g., 24 hour ECG).
- Must not introduce distortion, which may lead to wrong diagnosis.
- Formal evaluation is necessary.

# ECG Data Compression



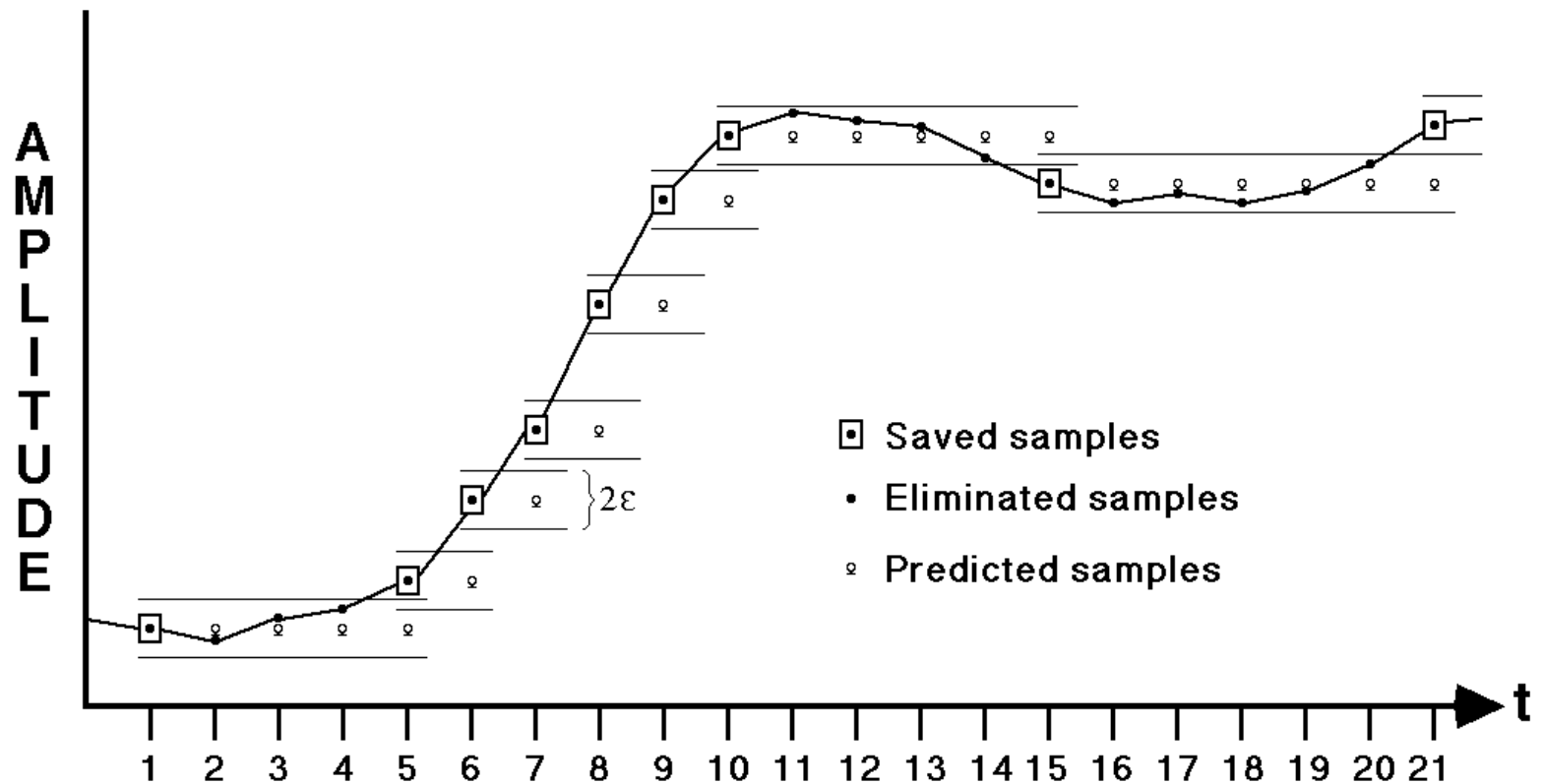
$$PRD = 100 \cdot \sqrt{\frac{\sum_{i=1}^n (\text{ORG}(i) - \text{REC}(i))^2}{\sum_{i=1}^n (\text{ORG}(i))^2}}$$

WGAQQQQQQRBCCCCCHZY

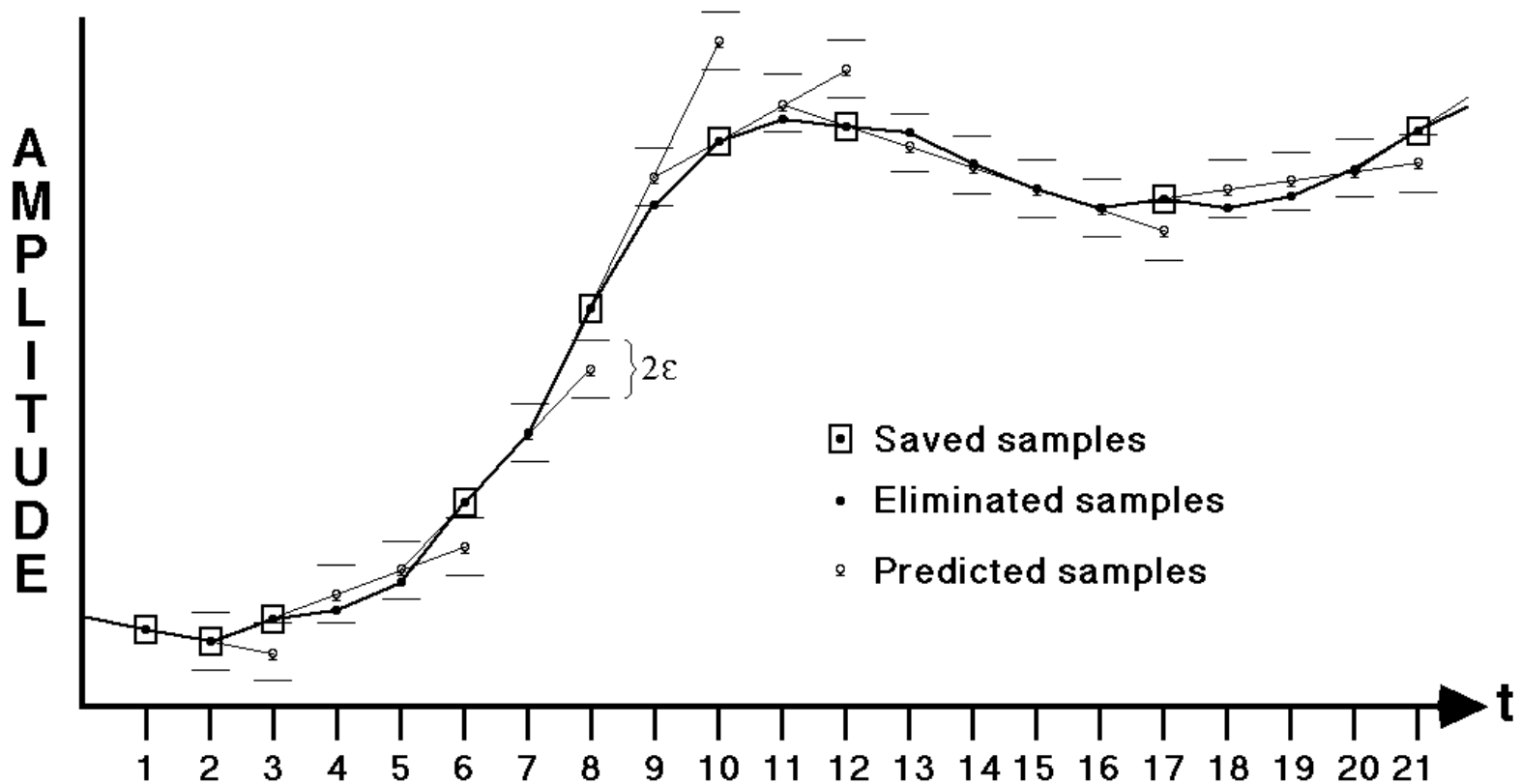


WGAQ\*6RBC\*5HZY

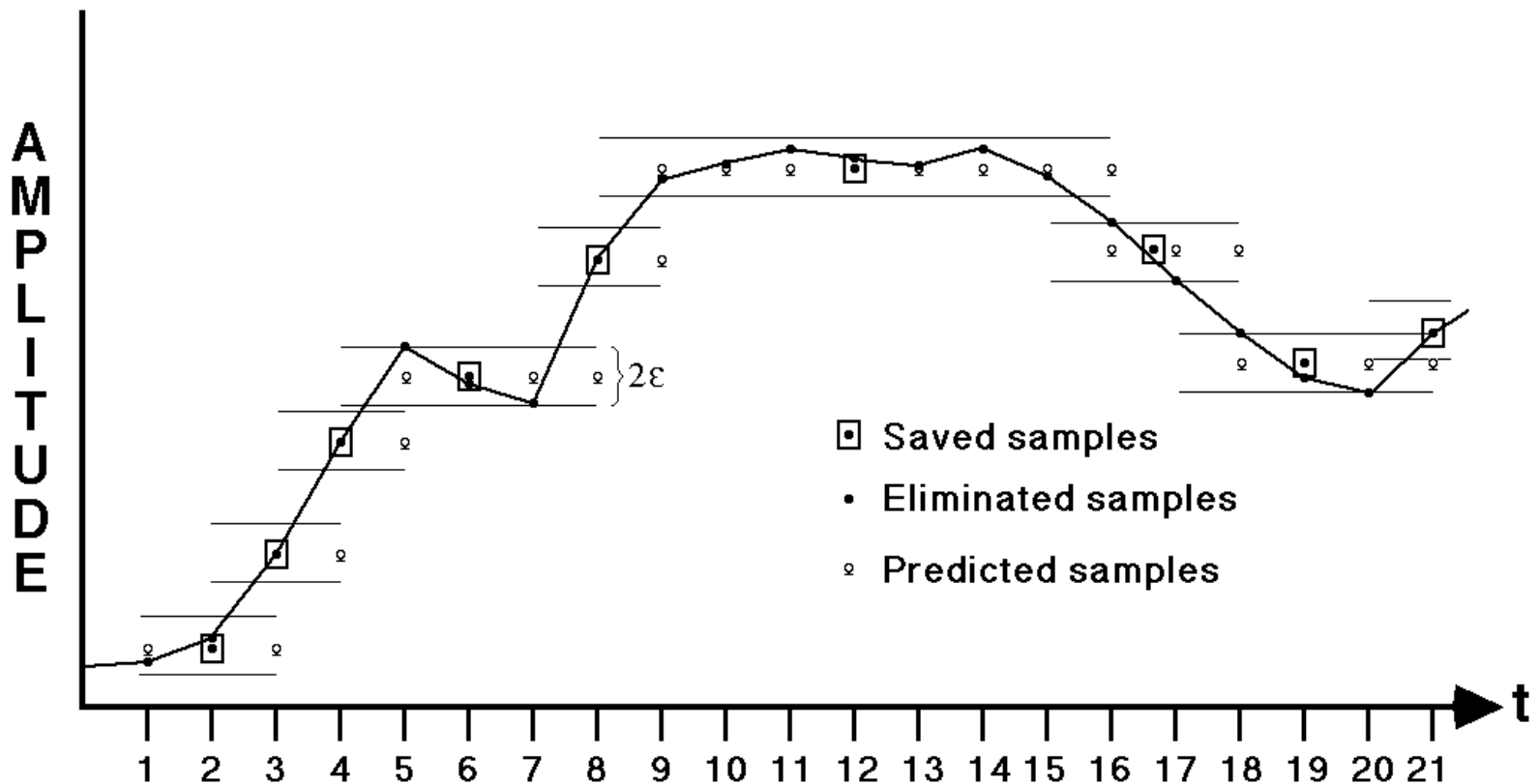
# ECG Data Compression



# ECG Data Compression



# ECG Data Compression

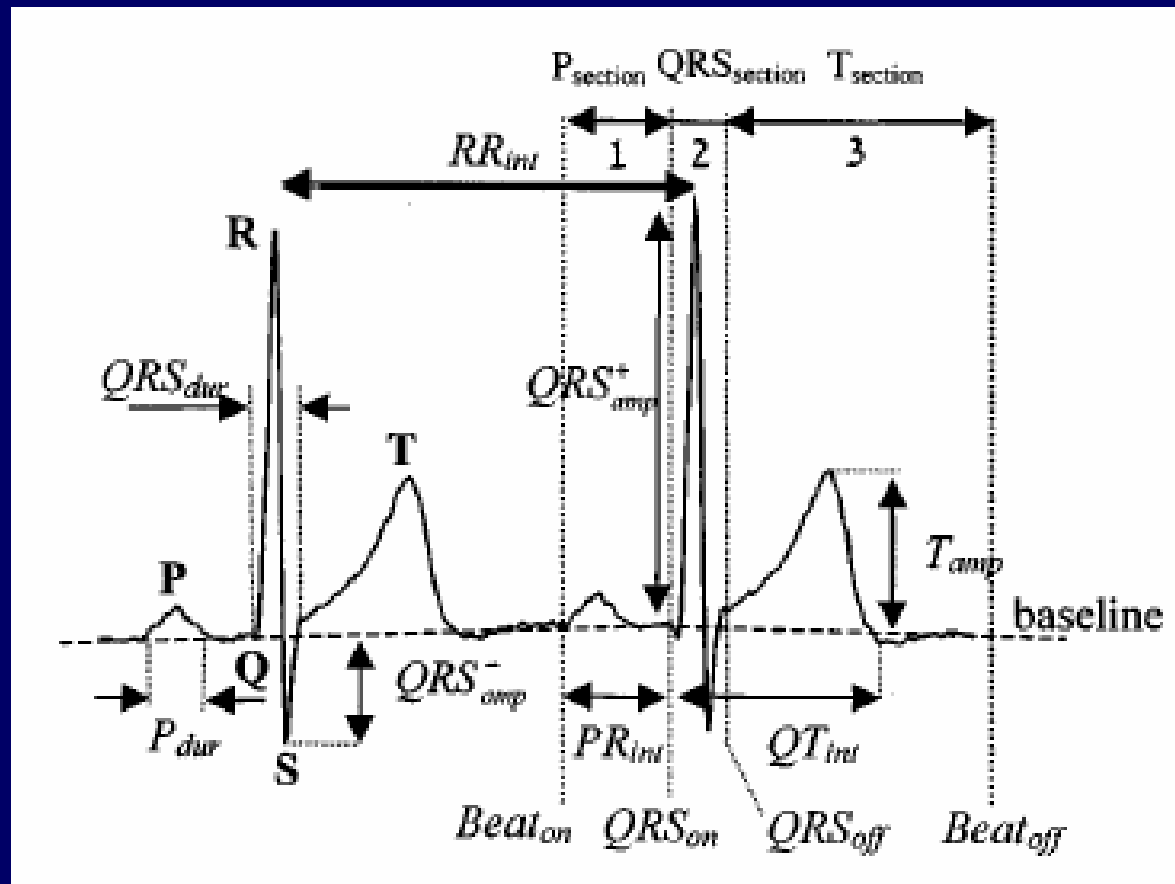


Is *straightforward*  
implementation sufficient for  
biomedical signals?



# Characteristics of Biomedical Signals (I): Weak $\neq$ Unimportant

- The information is in the details:



# OK!

## JPEG Compression



4302 Bytes



2245 Bytes



1714 Bytes



4272 Bytes



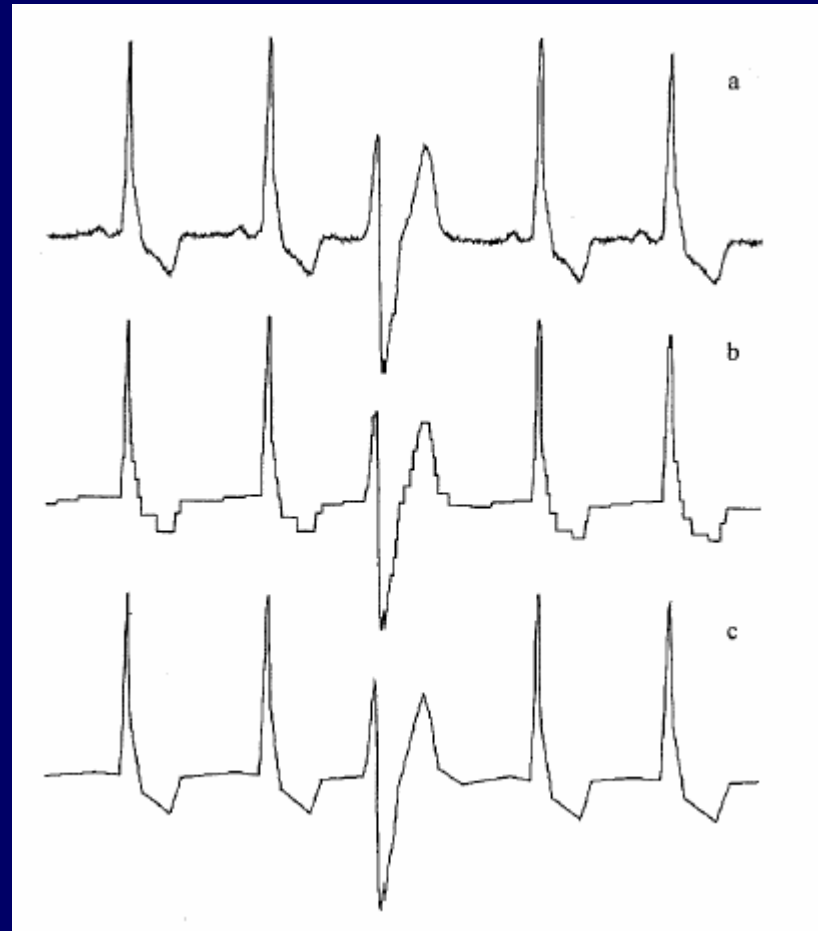
2256 Bytes



1708 Bytes

## Wavelet Compression

# OK?

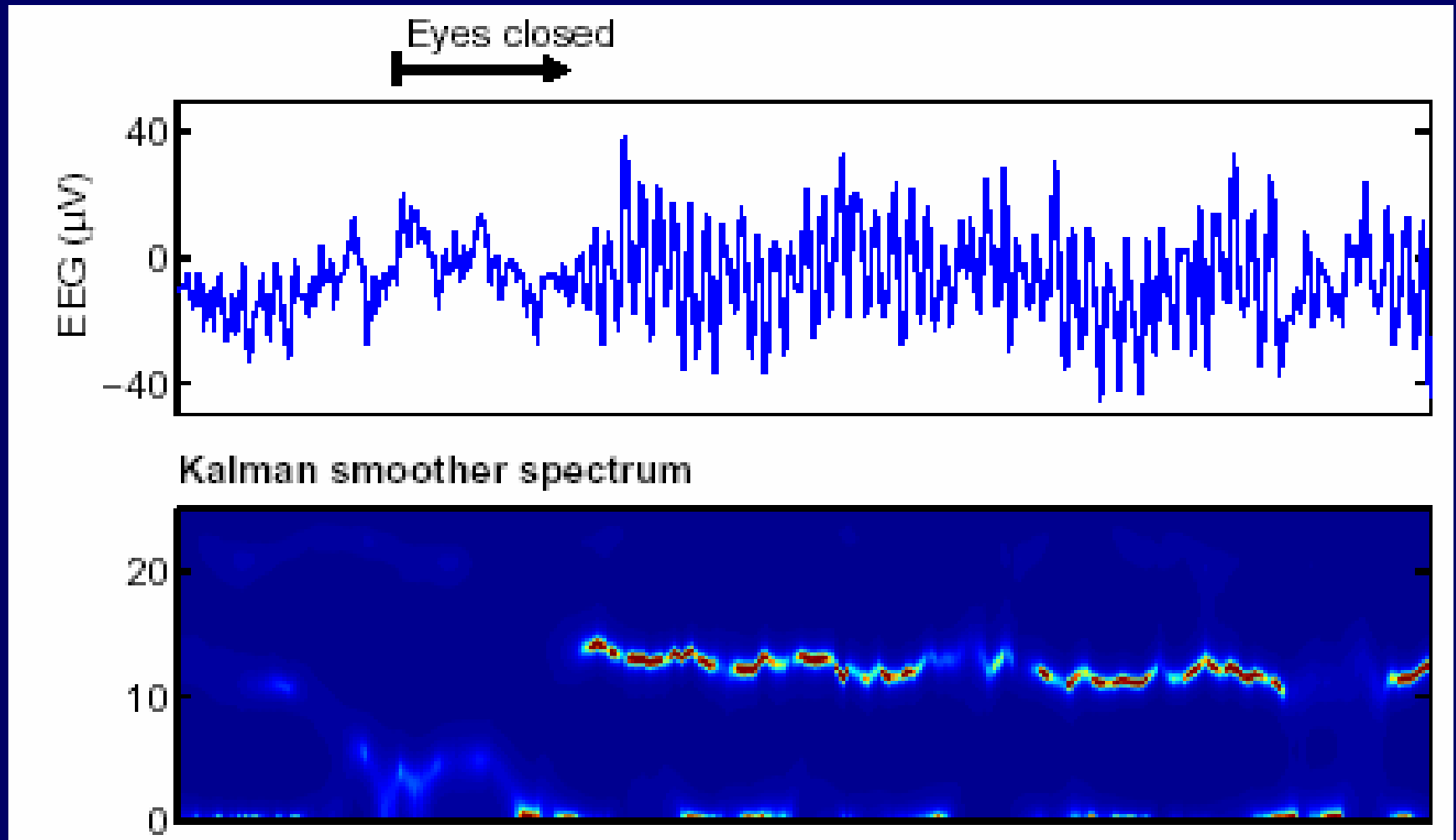


# Characteristics of Biomedical Signals (II): Nonstationarity

$$\text{Fourier Transform : } X(\omega) = \int_{-\infty}^{+\infty} x(t) e^{-j\omega t} dt$$

- Fourier transform requires signal stationarity.
- Biomedical signals are often time-varying.
  - Short-time Fourier analysis
  - Time-frequency representation
  - Cyclo-stationarity

# Nonstationarity: An EEG Example



# Spectral Estimation for Nonstationary Signals

- Fourier Transform  $\rightarrow$  Short Time Fourier Transform

$$X(\omega) = \int_{-\infty}^{+\infty} x(t) e^{-j\omega t} dt$$

$\Downarrow$

$$X(\omega, a) = \int_{-\infty}^{+\infty} x(t) g(t - a) e^{-j\omega t} dt$$

Another Example:  
Signal Processing for  
Blood Velocity Estimation  
(Please refer to the class notes.)

# Other Important Biomedical Applications

- Biomedical imaging:
  - X-ray, CT, MRI, PET, OCT, Ultrasound,...
- Genomic signal processing
- ...,etc

# Term Project

<http://ultrasound.ee.ntu.edu.tw>

課程→數位訊號處理概論